## **Get Ready for Chapter 5**

Diagnose Readiness You have two options for checking Prerequisite Skills.

**Text Option** 

Take the Quick Check below. Refer to the Quick Review for help.

### **Quick**Check

Evaluate each expression for the given values. (Lesson 1-2)

1. 
$$3x + y$$
 if  $x = -4$  and  $y = 2$ 

**2.** 
$$-2m + 3k$$
 if  $m = -8$  and  $k = 3$ 

**3. CARS** The expression 
$$\frac{m \text{ mi}}{g \text{ gal}}$$
 represents the gas mileage of a car. Find the gas mileage of a car that goes 295 miles on 12 gallons of gasoline. Round to the nearest tenth.

**Quick**Review

#### **EXAMPLE 1**

Evaluate  $-3x^2 + 4x - 6$  if x = -2.

$$-3x^2 + 4x - 6$$

**Original expression** 

$$= -3(-2)^2 + 4(-2) - 6$$

Replace x with -2.

$$= -3(4) + 4(-2) - 6$$
$$= -12 + (-8) - 6$$

**Evaluate the power.** 

Multiply.

$$= -26$$

Add and subtract.

Solve each equation. (Lesson 2-2)

**4.** 
$$x - 4 = 9$$

**5.** 
$$x + 8 = -3$$

**6.** 
$$4x = -16$$

7. 
$$\frac{x}{3} = 7$$

**8.** 
$$2x + 1 = 9$$

**8.** 
$$2x + 1 = 9$$
 **9.**  $4x - 5 = 15$ 

**10.** 
$$9x + 2 = 3x - 10$$

**11.** 
$$3(x-2) = -2(x+13)$$

12. FINANCIAL LITERACY Claudia opened a savings account with \$325. She saves \$100 per month. Write an equation to determine how much money *d*, she has after m months. (Lesson 2-1)

**EXAMPLE 2** 

Solve -2(x-4) = 7x - 19.

$$-2(x-4) = 7x - 19$$

**Original equation** 

$$-2x + 8 = 7x - 19$$

**Distributive Property** 

$$-2x + 8 + 2x = 7x - 19 + 2x$$
 Add 2x.

$$8 = 9x - 19$$
 Simplify.

$$8 + 19 = 9x - 19 + 19$$
 Add 19.

$$27 = 9x$$

Simplify.

$$3 = x$$

Divide by 3.

Solve each equation. (Lesson 2-5)

**13.** 
$$|x + 11| = 18$$

**13.** 
$$|x + 11| = 18$$
 **14.**  $|3x - 2| = 16$ 

**15. SURVEYS** In a survey, 32% of the people chose pizza as their favorite food. The results were reported to within 2% accuracy. What is the maximum and minimum percent of people who chose pizza? (Lesson 2-5)

**EXAMPLE 3** 

Solve |x - 4| = 9.

If 
$$|x - 4| = 9$$
, then  $x - 4 = 9$  or  $x - 4 = -9$ .

$$x - 4 = 9$$
 or

$$x - 4 = -9$$

$$x - 4 + 4 = 9 + 4$$
  $x - 4 + 4 = -9 + 4$ 

$$x = 13 \qquad \qquad x = -5$$

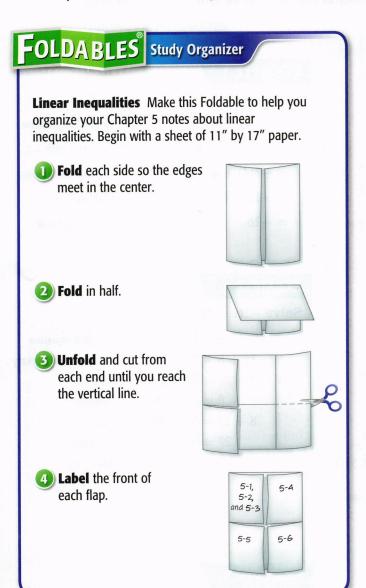
So, the solution set is  $\{-5, 13\}$ .

**Online Option** 

**Math Online** Take a self-check Chapter Readiness Quiz at glencoe.com.

## **Get Started on Chapter 5**

You will learn several new concepts, skills, and vocabulary terms as you study Chapter 5. To get ready, identify important terms and organize your resources. You may wish to refer to **Chapter 0** to review prerequisite skills.



### **New Vocabulary**

#### **English Español**

set-builder notation • p. 284 • notación de construcción de conjuntos

compound inequality • p. 304 • designaldad compuesta

intersection • p. 304 • intersección

union • p. 305 • unión

boundary • p. 315 • frontera

half-plane • p. 315 • semiplano

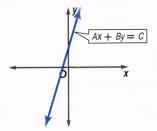
closed half-plane • p. 315 • semiplano cerrada

open half-plane • p. 315 • semiplano abierto

### **Review Vocabulary**

equivalent equations • p. 83 • ecuaciones equivalentes equations that have the same solution

**linear equation** • p. 153 • ecuación lineal an equation in the form Ax + By = C, with a graph consisting of points on a straight line



solution set • p. 31 • conjunto solución the set of elements from the replacement set that makes an open sentence true

Multilingual eGlossary glencoe.com

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- Use Extra Examples for additional help
- Take a Self-Check Quiz
- Review Vocabulary in fun ways

### Then

You solved equations by using addition and subtraction. (Lesson 2-2)

#### Now

- Solve linear inequalities by using addition.
- Solve linear inequalities by using subtraction.

#### New Vocabulary set-builder notation

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## **Solving Inequalities by Addition** and Subtraction

### Why?

The data in the table show that the recommended daily allowance of Calories for girls 11–14 years old is less than that of girls between 15–18 years old.

Calories				
Girls 11–14 Years	Girls 15–18			
1845	2110			

Source: Vital Health Zone

If a 13-year-old girl and a 16-year-old girl each eat 150 more Calories in a day than is suggested, the 16-year-old will still eat more Calories.



Solve Inequalities by Addition This example illustrates the Addition Property of Inequalities.

### **Key Concept**

#### **Addition Property of Inequalities**

**For Your** FOLDABLE

Words

If the same number is added to each side of a true inequality, the resulting inequality is also true.

**Symbols** 

For all numbers a, b, and c, the following are true.

1. If a > b, then a + c > b + c.

**2.** If a < b, then a + c < b + c.

This property is also true for  $\geq$  and  $\leq$ .

#### **EXAMPLE 1**

### **Solve by Adding**

Solve  $x - 12 \ge 8$ . Check your solution.

$$x-12 \ge 8$$
 Original inequality  $x-12+12 \ge 8+12$  Add 12 to each side. Simplify.

Simplify.

The solution is the set {all numbers greater than or equal to 20}.

**CHECK** To check, substitute three different values into the original inequality: 20, a number less than 20, and a number greater than 20.

### **Check Your Progress**

Solve each inequality. Check your solution.

**1A.** 
$$22 > m - 8$$

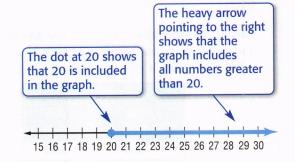
**1B.** 
$$d - 14 \ge -19$$

#### ReadingMath

set-builder notation  $\{x \mid x \geq 20\}$  is read the set of all numbers x such that x is greater than or equal to 20.

A more concise way of writing a solution set is to use set-builder notation. In set-builder notation, the solution set in Example 1 is  $\{x \mid x \ge 20\}$ .

This solution set can be graphed on a number line. Be sure to check if the endpoint of the graph of an inequality should be a circle or a dot. If the endpoint is not included in the graph, use a circle, otherwise use a dot.



Solve Inequalities by Subtraction Subtraction can also be used to solve inequalities.

### **Key Concept**

#### **Subtraction Property of Inequalities**

For Your FOLDABLE

Words

If the same number is subtracted from each side of a true inequality, the resulting inequality is also true.

Symbols

For all numbers a, b, and c, the following are true.

**1.** If 
$$a > b$$
, then  $a - c > b - c$ .

**2.** If 
$$a < b$$
, then  $a - c < b - c$ .

This property is also true for  $\geq$  and  $\leq$ .

#### Test-TakingTip

**Isolating the** Variable When solving inequalities, the goal is to isolate the variable on one side of the inequality. This is the same as with solving equations.

#### STANDARDIZED TEST EXAMPLE 2

Solve m + 19 > 56.

**A** 
$$\{m \mid m < 41\}$$

**B** 
$$\{m \mid m < 37\}$$

**A** 
$$\{m \mid m < 41\}$$
 **B**  $\{m \mid m < 37\}$  **C**  $\{m \mid m > 37\}$ 

**D** 
$$\{m \mid m > 41\}$$

#### Read the Test Item

You need to find the solution set for the inequality.

#### Solve the Test Item

**Step 1** Solve the inequality.

$$m + 19 > 56$$

**Original inequality** 

$$m + 19 - 19 > 56 - 19$$

Subtract 19 from each side.

Simplify.

**Step 2** Write in set-builder notation:  $\{m \mid m > 37\}$ . The answer is C.

### **Check Your Progress**

**2.** Solve  $p + 8 \le 18$ .

**F** 
$$\{p \mid p \ge 10\}$$

**G** 
$$\{p \mid p \le 10\}$$

**H** 
$$\{p \mid p \le 26\}$$

J 
$$\{p \mid p \ge 126\}$$

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#### StudyTip

#### **Writing Inequalities**

Simplifying the inequality so that the variable is on the left side, as in  $a \ge 6$ , prepares you to write the solution set in set-builder notation.

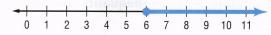
Terms that are constants are not the only terms that can be subtracted. Terms with variables can also be subtracted from each side to solve inequalities.

### **EXAMPLE 3** Variables on Each Side

Solve  $3a + 6 \le 4a$ . Then graph the solution set on a number line.

$$3a + 6 \le 4a$$
 Original inequality  $3a - 3a + 6 \le 4a - 3a$  Subtract  $3a$  from each side. Simplify.

Since  $6 \le a$  is the same as  $a \ge 6$ , the solution set is  $\{a \mid a \ge 6\}$ .



### Check Your Progress

Solve each inequality. Then graph the solution set on a number line.

**3A.** 
$$9n - 1 < 10n$$

**3B.** 
$$5h \le 12 + 4h$$

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Verbal problems containing phrases like *greater than* or *less than* can be solved by using inequalities. The chart shows some other phrases that indicate inequalities.

Concept Sum	For Your FOLDABLE		
<	>	≤	2
less than fewer than	greater than more than	at most, no more than, less than or equal to	at least, no less than, greater than or equal to

### Real-World EXAMPLE 4 Use an Inequality to Solve a Problem

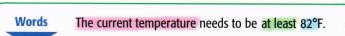
PETS Felipe needs for the temperature of his leopard gecko's basking spot to be at least 82°F. Currently the basking spot is 62.5°F. How much warmer does the basking spot need to be?



#### Real-World Link

Leopard geckos are commonly yellow and white with black spots. They are nocturnal and easy to tame. They do not have toe pads like other geckos, so they do not climb.

Source: Exotic Pets



**Variable** 

Let t = the number of degrees that the temperature needs to rise.

Inequality

62.5 + t

82

$$62.5 + t \ge 82$$
 Original inequality Subtract 62.5 from each side.  $t \ge 19.5$  Simplify.

Felipe needs to raise the temperature of the basking spot 19.5°F or more.

### **Check Your Progress**

**4. SHOPPING** Sanjay has \$65 to spend at the mall. He bought a T-shirt for \$18 and a belt for \$14. If Sanjay wants a pair of jeans, how much can he spend?

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### **Check Your Understanding**

#### Examples 1 and 2 pp. 283-284

Solve each inequality. Then graph the solution set on a number line.

1. 
$$x - 3 > 7$$

3. 
$$g + 6 < 2$$

5. 
$$10 > n - 1$$

7. 
$$8r + 6 < 9r$$

**2.** 
$$5 \ge 7 + y$$

**4.** 
$$11 \le p + 4$$

**6.** 
$$k + 24 > -5$$

**8.** 
$$8n \ge 7n - 3$$

#### Example 3 p. 285

Define a variable, write an inequality, and solve each problem. Check your solution.

- **9.** A number increased by 4 is at least 10.
- **10.** Three more than a number is less than twice the number.

#### **Example 4** p. 285

11. AMUSEMENT A thrill ride swings passengers back and forth, a little higher each time up to 137 feet. Suppose the height of the swing after 30 seconds is 45 feet. How much higher will the ride swing?

### **Practice and Problem Solving**



#### **Examples 1 and 2** pp. 283-284

Solve each inequality. Then graph the solution set on a number line.

**12.** 
$$m - 4 < 3$$

13) 
$$p - 6 \ge 3$$

**14.** 
$$r - 8 \le 7$$

**15.** 
$$t - 3 > -8$$

**16.** 
$$b + 2 \ge 4$$

17. 
$$13 > 18 + r$$

**18.** 
$$5 + c \le 1$$

**19.** 
$$-23 \ge q - 30$$

**20.** 
$$11 + m \ge 15$$

**21.** 
$$h - 26 < 4$$

**22.** 
$$8 \le r - 14$$

**23.** 
$$-7 > 20 + c$$

**24.** 
$$2a \le -4 + a$$

**25.** 
$$z + 4 \ge 2z$$

**26.** 
$$w - 5 \le 2w$$

**27.** 
$$3y + 6 \le 2y$$

**28.** 
$$6x + 5 \ge 7x$$

**29.** 
$$-9 + 2a < 3a$$

#### Example 3 p. 285

Define a variable, write an inequality, and solve each problem. Check your solution.

- **30.** The sum of a number and -4 is at least 8.
- **31.** A number decreased by 8 is less than 21.
- **32.** Twice a number is more than the sum of that number and 9.
- **33.** The sum of twice a number and 5 is at most 3 less than the number.

#### **Example 4** p. 285

Define a variable, write an inequality, and solve each problem. Then interpret your solution.

- **34. FINANCIAL LITERACY** Keisha is babysitting at \$8 per hour to earn money for a car. So far she has saved \$1300. The car that Keisha wants to buy costs at least \$5440. How much money does Keisha still need to earn to buy the car?
- **35. TECHNOLOGY** A recent survey found that more than 21 million people between the ages of 12 and 17 use the Internet. Of those, about 16 million said they use the Internet at school. How many teens that are online do not use the Internet at school?
- **36.** MUSIC A DJ added 20 more songs to his MP3 player, making the total more than 61. How many songs were originally on the player?



#### Real-World Link

In a recent year, 55% of American teenagers said they volunteered within the last year, nearly double the percentage of adults.

Source: Corporation for National and Community Service

- **37. TEMPERATURE** The water temperature in a swimming pool increased 4°F this morning. The temperature is now less than 81°F. What was the water temperature this morning?
- 38. BASKETBALL A player's goal was to score at least 150 points this season. So far, she has scored 123 points. If there is one game left, how many points must she score to reach her goal?
- SPAS Samantha received a \$75 gift card for a local day spa for her birthday. She plans to get a haircut and a manicure. How much money will be left on her gift card after her visit?

Service	Cost (\$)
haircut	at least 32
manicure	at least 26

**40. VOLUNTEER** Kono knows that he can only volunteer up to 25 hours per week. If he has volunteered for the times recorded at the right, how much more time can Kono volunteer this week?

Center	Time (h)
Shelter	3 h 15 min
Kitchen	2 h 20 min

Solve each inequality. Check your solution, and then graph it on a number line.

**41.** 
$$c + (-1.4) \ge 2.3$$

**42.** 
$$9.1g + 4.5 < 10.1g$$

**43.** 
$$k + \frac{3}{4} > \frac{1}{3}$$

**44.** 
$$\frac{3}{2}p - \frac{2}{3} \le \frac{4}{9} + \frac{1}{2}p$$

- 45. MULTIPLE REPRESENTATIONS In this problem, you will explore multiplication and division in inequalities.
  - **a. GEOMETRIC** Suppose a balance has 12 pounds on the left side and 18 pounds on the right side. Draw a picture to represent this situation.
  - **b. NUMERICAL** Write an inequality to represent the situation.
  - c. TABULAR Create a table showing the result of doubling, tripling, or quadrupling the weight on each side of the balance. Create a second table showing the result of reducing the weight on each side of the balance by a factor of  $\frac{1}{2}$ ,  $\frac{1}{3}$ , or  $\frac{1}{4}$ . Include a column in each table for the inequality representing each situation.
  - **d. VERBAL** Describe the effect multiplying or dividing each side of an inequality by the same positive value has on the inequality.

If  $m + 7 \ge 24$ , then complete each inequality.

**47.** 
$$m + ? \ge 27$$

**48.** 
$$m-5 \ge \underline{?}$$

**49.** 
$$m - ? \ge 14$$

**50.** 
$$m - 19 \ge ?$$

**51.** 
$$m + ? \ge 43$$

### **H.O.T. Problems**

Use Higher-Order Thinking Skills

- **52. REASONING** Compare and contrast the graphs of a < 4 and  $a \le 4$ .
- **53. CHALLENGE** Suppose  $b > d + \frac{1}{3}$ , c + 1 < a 4, and  $d + \frac{5}{8} > a + 2$ . Order a, b, c, and d from least to greatest.
- **54. OPEN ENDED** Write three linear inequalities that are equivalent to y < -3.
- **55. WRITING IN MATH** Summarize the process of solving and graphing linear inequalities.
- **56.** WRITING IN MATH Explain why x 2 > 5 has the same solution set as x > 7.

### Standardized Test Practice

**57.** Which equation represents the relationship shown?

A	U	=	7x	_	8

**B** 
$$y = 7x + 8$$

**C** 
$$y = 8x - 7$$

**D** 
$$y = 8x + 7$$

X	y
1	1
2	9
3	17
4	25
5	33
6	41

**58.** What is the solution set of the inequality 7 + x < 5?

$$\mathbf{F} \{ \mathbf{r} \mid \mathbf{r} < 2 \}$$

**F** 
$$\{x \mid x < 2\}$$

**H** 
$$\{x \mid x < -2\}$$

**G** 
$$\{x \mid x > 2\}$$

$$\mathbf{J} \quad \{x \mid x > -2\}$$

**59.** Francisco has \$3 more than  $\frac{1}{4}$  the number of dollars that Kayla has. Which expression represents how much money Francisco has?

A 
$$3\left(\frac{1}{4}k\right)$$

**A** 
$$3(\frac{1}{4}k)$$
 **C**  $3-\frac{1}{4}k$ 

**B** 
$$\frac{1}{4}k + 3$$
 **D**  $\frac{1}{4} + 3k$ 

**D** 
$$\frac{1}{4} + 3k$$

**60. GRIDDED RESPONSE** The mean score for 10 students on the chemistry final exam was 178. However, the teacher had made a mistake and recorded one student's score as ten points less than the actual score. What should the mean score be?

### **Spiral Review**

Graph each function. (Lesson 4-7)

**61.** 
$$f(x) = |3x + 2|$$

**63.** 
$$f(x) = [x + 1]$$

**62.** 
$$f(x) = \begin{cases} x - 2 \text{ if } x > -1 \\ x + 3 \text{ if } x \le -1 \end{cases}$$

**64.** 
$$f(x) = \left| \frac{1}{4}x - 1 \right|$$

Write the slope-intercept form of an equation for the line that passes through the given point and is perpendicular to the graph of each equation. (Lesson 4-4)

**65.** 
$$(-2, 0), y = x - 6$$

**67.** 
$$(1, -3), y = \frac{1}{2}x + 4$$

**66.** 
$$(-3, 1), y = -3x + 7$$

**68.** 
$$(-2,7)$$
,  $2x - 5y = 3$ 

**69. TRAVEL** On an island cruise in Hawaii, each passenger is given a lei. A crew member hands out 3 red, 3 blue, and 3 green leis in that order. If this pattern is repeated, what color lei will the 50th person receive? (Lesson 3-6)

Find the *n*th term of each arithmetic sequence described. (Lesson 3-5)

**70.** 
$$a_1 = 52$$
,  $d = 12$ ,  $n = 102$ 

**71.** 
$$-9, -7, -5, -3, \dots$$
 for  $n = 18$ 

**72.** 0.5, 1, 1.5, 2, ... for 
$$n = 50$$

73. JOBS Refer to the time card shown. Write a direct variation equation relating your pay to the hours worked and find your pay if you work 30 hours. (Lesson 3-4)

Weekly Time Card				
Day	Hours			
FRIDAY	2.0			
SATURDAY	3.5			
SUNDAY	2.0			
TOTAL HOURS	7.5			
PAY	\$52.50			

### Skills Review

Solve each equation. (Lesson 2-2)

**74.** 
$$8y = 56$$

**75.** 
$$4p = -120$$

**76.** 
$$-3a = -21$$

**77.** 
$$2c = \frac{1}{5}$$
  
**81.**  $-6x = \frac{2}{3}$ 

**78.** 
$$\frac{r}{2} = 21$$

**79.** 
$$-\frac{3}{4}g = -12$$

**80.** 
$$\frac{2}{5}w = -4$$

**81.** 
$$-6x = \frac{2}{3}$$

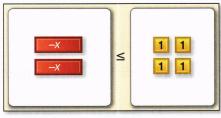
You can use algebra tiles to solve inequalities.

**ACTIVITY** 

**Solve Inequalities** 

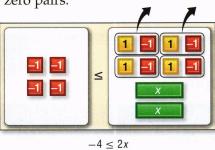
Solve -2x ≤ 4.

**Step 1** Use a self-adhesive note to cover the equals sign on the equation mat. Then write a  $\leq$  symbol on the note. Model the inequality.

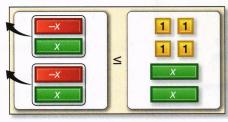


 $-2x \leq 4$ 

**Step 3** Add 4 negative 1-tiles to each side to isolate the *x*-tiles. Remove the zero pairs.

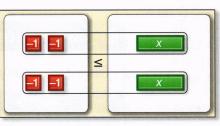


**Step 2** Since you do not want to solve for a negative x-tile, eliminate the negative xtiles by adding 2 positive x-tiles to each side. Remove the zero pairs.



 $-2x + 2x \le 4 + 2x$ 

**Step 4** Separate the tiles into 2 groups.



 $-2 \le x \text{ or } x \ge -2$ 

### **Model and Analyze**

Use algebra tiles to solve each inequality.

1. 
$$-3x < 9$$

**2.** 
$$-4x > -4$$

**3.** 
$$-5x \ge 15$$

**4.** 
$$-6x \le -12$$

- **5.** In Exercises 1–4, is the coefficient of x in each inequality positive or negative?
- **6.** Compare the inequality symbols and locations of the variable in Exercises 1–4 with those in their solutions. What do you find?
- **7.** Model the solution for  $3x \le 12$ . How is this different from solving  $-3x \le 12$ ?
- **8.** Write a rule for solving inequalities involving multiplication and division. (Hint: Remember that dividing by a number is the same as multiplying by its reciprocal.)

### Then

You solved equations by using multiplication and division. (Lesson 2-3)

#### Now

- Solve linear inequalities by using multiplication.
- Solve linear inequalities by using division.

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**Solving Inequalities by Multiplication and Division** 

### Why

Terrell received a gift card for \$20 of music downloads. If each download costs \$0.89, the number of downloads he can purchase can be represented by the inequality  $0.89d \le 20$ .

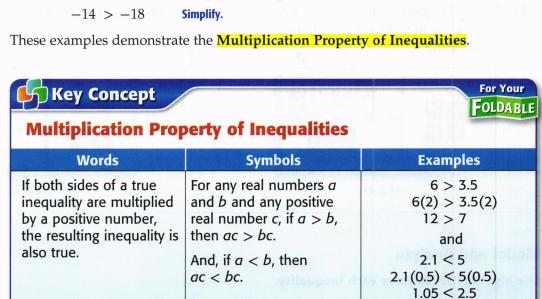
**Solve Inequalities by Multiplication** If you multiply each side of an inequality by a positive number, then the inequality remains true.

$$4 > 2$$
 Original inequality  $4(3) \stackrel{?}{\underline{?}} 2(3)$  Multiply each side by 3.  $12 > 6$  Simplify.

Notice that the direction of the inequality remains the same.

If you multiply each side of an inequality by a negative number, the inequality symbol changes direction.

$$7 < 9$$
 Original inequality  $7(-2) \stackrel{?}{\underline{?}} 9(-2)$  Multiply each side by  $-2$ . Simplify.



inequality sign is 3.1 < 5.2And, if a < b, then reversed to make the 3.1(-4) > 5.2(-4)ac > bc. resulting inequality -12.4 > -20.8

7 > 4.57(-3) < 4.5(-3)

-21 < -13.5

and

This property also holds for inequalities involving  $\leq$  and  $\geq$ .

For any real numbers a

and b and any negative real number c, if a > b,

then ac < bc.

If both sides of a true

inequality are multiplied

by a negative number, the direction of the

also true.

#### StudyTip

**Checking Solutions** In Example 1, you could also check the solution by substituting a number greater than 672 and verifying that the resulting inequality is false.



#### Real-World Link

More than 30,000 different orchid species flower in the wild on every continent except Antarctica.

Source: Aloha Orchid Nursery

#### Real-World EXAMPLE 1

### Write and Solve an Inequality

SURVEYS Of the students surveyed at Madison High School, fewer than eightyfour said they have never purchased an item online. This is about one eighth of those surveyed. How many students were surveyed?

**Understand** You know the number of students who have never purchased an item online and the portion this is of the number of students surveyed.

**Plan** Let n = the number of students surveyed. Write an open sentence that represents this situation.

Words	One eighth	times	the number of students surveyed	is less than	84.
Inequality	$\frac{1}{8}$	•	n	<	84.

**Solve** Solve for n.

$$\frac{1}{8}n < 84$$
 Original inequality

(8)  $\frac{1}{8}n <$  (8)84 Multiply each side by 8.

 $n < 672$  Simplify.

**Check** To check this answer, substitute a number less than 672 into the original inequality. If n = 80, then  $\frac{1}{8}(80)$  or 10 < 84, so the solution checks.

The solution set is  $\{n \mid n < 672\}$ , so fewer than 672 students were surveyed at Madison High School.

### **Check Your Progress**

1. **BIOLOGY** Mount Kinabalue in Malaysia has the greatest concentration of wild orchids on Earth. It contains more than 750 species, or about one fourth of all orchid species in Malaysia. How many orchid species are there in Malaysia?

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You can also use multiplicative inverses with the Multiplication Property of Inequalities to solve an inequality.

### **EXAMPLE 2** Solve by Multiplying

Solve  $-\frac{3}{7}r < 21$ . Check your solution.

$$-\frac{3}{7}r < 21$$

**Original inequality** 

$$\left(-\frac{7}{3}\right)\left(-\frac{3}{7}r\right) > 21\left(-\frac{7}{3}\right)$$

 $\left(-\frac{7}{3}\right)\left(-\frac{3}{7}r\right) > 21\left(-\frac{7}{3}\right)$  Multiply each side by  $-\frac{7}{3}$ . Reverse the inequality symbol.

Simplify. Check by substituting values.

The solution set is  $\{r \mid r > -49\}$ .



**Check Your Progress** Solve each inequality. Check your solution.

**2A.** 
$$-\frac{n}{6} \le 8$$

**2B.** 
$$-\frac{4}{3}p > -10$$
  
**2D.**  $\frac{3}{8}t < 5$ 

**2A.** 
$$-\frac{n}{6} \le 8$$
 **2C.**  $\frac{1}{5}m \ge -3$ 

**2D.** 
$$\frac{3}{8}t < 5$$

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#### Watch Out!

**Negatives** A negative sign in an inequality does not necessarily mean that the direction of the inequality should change. For example, when solving  $\frac{x}{6} > -3$ , do not change the direction of the inequality.

**Solve Inequalities by Division** If you divide each side of an inequality by a positive number, then the inequality remains true.

$$-10 < -5$$
 Original inequality
 $\frac{-10}{5} \stackrel{?}{=} \frac{-5}{5}$  Divide each side by -5.
 $-2 < -1$  Simplify.

Notice that the direction of the inequality remains the same. If you divide each side of an inequality by a negative number, the inequality symbol changes direction.

$$\begin{array}{c|c} 15 < 18 & \text{Original inequality} \\ \hline 15 \\ \hline -3 & ? \\ \hline -5 > -6 & \text{Simplify.} \end{array}$$

These examples demonstrate the **Division Property of Inequalities.** 

Key Concept			For Your OLDABLE
<b>Division Property</b>	of Inequalities	L.	CESABLE
Words	Symbols	Examples	
If both sides of a true inequality are divided by a positive number, the resulting inequality is also true.	For any real numbers $a$ and $b$ and any positive real number $c$ , if $a > b$ , then $\frac{a}{c} > \frac{b}{c}$ . And, if $a < b$ , then $\frac{a}{c} < \frac{b}{c}$ .	$4.5 > 2.1  \frac{4.5}{3} > \frac{2.1}{3} \text{ and } \frac{1.5}{0.5} < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0.5 < 0$	
If both sides of a true inequality are divided by a negative number, the direction of the inequality sign is reversed to make the resulting inequality also true.	For any real numbers $a$ and $b$ and any negative real number $c$ , if $a > b$ , then $\frac{a}{c} < \frac{b}{c}$ . And, if $a < b$ , then $\frac{a}{c} > \frac{b}{c}$ .	$\frac{6}{-6} < \frac{2.4}{-6}$ and $\frac{-1.8}{-9}$	$< 3.6$ $< \frac{3.6}{-9}$ $> -0.4$

This property also holds for inequalities involving  $\leq$  and  $\geq$ .

### **EXAMPLE 3** Divide to Solve an Inequality

Solve each inequality. Check your solution.

a. 
$$60t > 8$$

$$60t > 8$$

$$60t > 8$$

$$\frac{60t}{60} > \frac{8}{60}$$

$$t > \frac{2}{15}$$

$$(t \mid t > \frac{2}{15})$$
Original inequality
$$\frac{60t}{-7} \le \frac{147}{-7}$$
Divide each side by 60.
$$\frac{-7d}{-7} \ge \frac{147}{-7}$$
Divide each side by -7.
$$d \ge -21$$
Simplify.
$$(d \mid d \ge -21)$$



**3A.** 
$$8p < 58$$
 **3B.**  $-42 > 6r$  **3C.**  $-12h > 15$  **3D.**  $-\frac{1}{2}n < 6$ 

### Check Your Understanding

### **Example 1**

p. 291

1. FUNDRAISING The Jefferson Band Boosters raised more than \$5500 from sales of their \$15 band DVD. Define a variable, and write an inequality to represent the number of DVDs they sold. Solve the inequality and interpret your solution.

### **Examples 2 and 3**

pp. 291-292

Solve each inequality. Check your solution.

**2.** 
$$30 > \frac{1}{2}n$$

**2.** 
$$30 > \frac{1}{2}n$$
 **3.**  $-\frac{3}{4}r \le -6$  **4.**  $-\frac{c}{6} \ge 7$  **5.**  $\frac{h}{2} < -5$ 

**4.** 
$$-\frac{c}{6} \ge 7$$

**5.** 
$$\frac{h}{2} < -5$$

**6.** 
$$9t > 108$$

**6.** 
$$9t > 108$$
 **7.**  $-84 < 7v$ 

**8.** 
$$-28 \le -6x$$

**9.** 
$$40 \ge -5z$$

### **Practice and Problem Solving**



Step-by-Step Solutions begin on page R12. Extra Practice begins on page 815.

#### **Example 1**

p. 291

Define a variable, write an inequality, and solve each problem. Then interpret your solution.

- 10. CELL PHONE PLAN Mario purchases a prepaid phone plan for \$50 at \$0.13 per minute. How many minutes can Mario talk on this plan?
- 11. FINANCIAL LITERACY Rodrigo needs at least \$560 to pay for his spring break expenses, and he is saving \$25 from each of his weekly paychecks. How long will it be before he can pay for his trip?

#### **Examples 2 and 3** pp. 291-292

Solve each inequality. Check your solution.

**12.** 
$$\frac{1}{4}m \le -17$$

$$\frac{1}{2}a < 20$$

**14.** 
$$-11 > -\frac{c}{11}$$

**15.** 
$$-2 \ge -\frac{d}{34}$$

**16.** 
$$-10 \le \frac{x}{-2}$$

17. 
$$-72 < \frac{f}{-6}$$

**18.** 
$$\frac{2}{3}h > 14$$

**19.** 
$$-\frac{3}{4}j \ge 12$$

**20.** 
$$-\frac{1}{6}n \le -18$$

**22.** 
$$4r < 64$$

**23.** 
$$32 > -2y$$

**24.** 
$$-26 < 26t$$

**25.** 
$$-6v > -72$$

**26.** 
$$-33 \ge -3z$$

**27.** 
$$4b \le -3$$

**28.** 
$$-2d < 5$$

**29.** 
$$-7f > 5$$



- **30.** CHEERLEADING To remain on the cheerleading squad, Lakita must attend at least  $\frac{3}{5}$ of the study table sessions offered. She attends 15 sessions. If Lakita met the requirements, what is the least amount of study table sessions?
- **31. BRACELETS** How many bracelets can Caitlin buy for herself and her friends if she wants to spend no more than \$22?
  - **32.** CHARITY The National Honor Society at Pleasantville High School wants to raise at least \$500 for a local charity. Each student earns \$0.50 for every quarter of a mile walked in a walk-a-thon. How many miles will the students need to walk?
  - **33. MUSEUM** The American history classes are planning a trip to a local museum. Admission is \$8 per person. Determine how many people can go for \$260.
  - **34. GASOLINE** If gasoline costs \$3.15 per gallon, how many gallons of gasoline, to the nearest tenth, can Jan buy for \$24?

Math History Link

Harriot was a prolific astronomer. He was the first to map the moon's surface and to see sunspots. Harriot is best known for his work in algebra.



#### Real-World Link

At the FedNor Pavillion Royal Winter Fair in Toronto, Canada, the Northwest Fudge Factory made the world's largest slab of fudge. The fudge weighed 3010 pounds.

Source: Guinness World

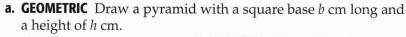
Match each inequality to the graph of its solution.

**35.** 
$$-\frac{2}{3}h \le 9$$

**37.** 
$$3.6p < -4.5$$
 **38.**  $2.3 < -5t$ 

-18 - 17 - 16 - 15 - 14 - 13 - 12 - 11 - 10 - 9 - 8

- **CANDY** Fewer than 42 employees at a factory stated that they preferred fudge over fruit candy. This is about two thirds of the employees. How many employees are there?
- **40. TRAVEL** A certain travel agency employs more than 275 people at all of its branches. Approximately three fifths of all the people are employed at the west branch. How many people work at the west branch?
- **41. MULTIPLE REPRESENTATIONS** The equation for the volume of a pyramid is  $\frac{1}{3}$  the area of the base times the height.





- **b. NUMERICAL** Suppose the pyramid has a volume of 72 cm<sup>3</sup>. Write an equation to find the height.
- **c. TABULAR** Create a table showing the value of h when b = 1, 3, 6, 9, and 12.
- **d. NUMERICAL** Write an inequality for the possible lengths of b such that b < h. Write an inequality for the possible lengths of h such that b > h.

### H.O.T. Problems

Use Higher-Order Thinking Skills

**42. FIND THE ERROR** Taro and Jamie are solving  $6d \ge -84$ . Is either of them correct? Explain your reasoning.

Tavo
$$6\lambda \ge -84$$

$$\frac{6\lambda}{6} \ge \frac{-84}{6}$$

$$\lambda \ge -14$$

Jamie
$$6d \ge -84$$

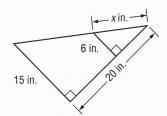
$$\frac{6d}{6} \le \frac{-84}{6}$$

$$d \le -14$$

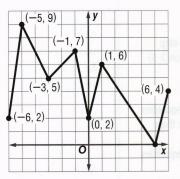
- **43. CHALLENGE** Solve -96c < 12d for *c* using two methods. Show your work.
- **44. CHALLENGE** Determine whether  $x^2 > 1$  and x > 1 are equivalent. Explain.
- **45. REASONING** Explain whether the statement If a > b, then  $\frac{1}{a} > \frac{1}{b}$  is sometimes, always, or never true.
- **46. OPEN ENDED** Create a real-world situation to represent the inequality  $-\frac{5}{9} \ge x$ .
- 47. WRITING IN MATH Explain the circumstances under which the inequality symbol changes directions. Use examples to support your explanation.

### **Standardized Test Practice**

- 48. Juan's long-distance phone company charges 9¢ for each minute. Which inequality can be used to find how long he can talk to a friend if he does not want to spend more than \$2.50 on the call?
  - **A**  $0.09 \ge 2.50m$
  - **B**  $0.09 \le 2.50m$
  - **C**  $0.09m \ge 2.50$
  - **D**  $0.09m \le 2.50$
- **49. SHORT RESPONSE** Find the value of x.



**50.** What is the greatest rate of decrease of this function?



- $\mathbf{F}$  -5
- H-2
- G -3
- J 1
- **51.** What is the value of x if 4x 3 = -2x?
  - A -2
- **B**  $-\frac{1}{2}$
- D 2

### **Spiral Review**

Solve each inequality. Check your solution, and then graph it on a number line. (Lesson 5-1)

**52.** 
$$-8 + 4a < 6a$$

**53.** 
$$2y + 11 \ge -24y$$

**54.** 
$$7 - 2b > 12b$$

Determine the domain and range for each function. (Lesson 4-7)

**55.** 
$$f(x) = |2x - 5|$$

**56.** 
$$h(x) = |x - 1|$$

**57.** 
$$g(x) = \begin{cases} -3x + 4 \text{ if } x > 2\\ x - 1 \text{ if } x \le 2 \end{cases}$$

- **58. HOME DECOR** Pam is having blinds installed at her home. The cost c of installation for any number of blinds b can be described by c = 25 + 6.5b. Graph the equation and determine how much it would cost if Pam has 8 blinds installed. (Lesson 3-1)
- **59. RESCUE** A boater radioed for a helicopter to pick up a sick crew member. At that time, the boat and the helicopter were at the positions shown. How long will it take for the helicopter to reach the boat? (Lesson 2-8)



Solve each open sentence. (Lesson 2-5)

**60.** 
$$|x + 3| = 10$$

**61.** 
$$|2x - 8| = 6$$

**62.** 
$$|3x + 1| = -2$$

### **Skills Review**

Solve each equation. (Lessons 2-3 and 2-4)

**63.** 
$$4y + 11 = 19$$

**64.** 
$$2x - 7 = 9 + 4x$$

**65.** 
$$\frac{1}{4} + 2x = 4x - 8$$

**66.** 
$$\frac{1}{3}(6w - 3) = 3w + 12$$

**67.** 
$$\frac{7r+5}{2}=13$$

**65.** 
$$\frac{2}{4} + 2x = 4x - 8$$
  
**68.**  $\frac{1}{2}a = \frac{a-3}{4}$ 

# 5-3

#### Then

You solved multi-step equations. (Lesson 2-3)

#### Now

- Solve linear inequalities involving more than one operation.
- Solve linear inequalities involving the Distributive Property.

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- Personal Tutor
- Self-Check Quiz
- Homework Help
- Math in Motion

## **Solving Multi-Step Inequalities**

### Why?

A salesperson may make a base monthly salary and earn a commission on each of her sales. To find the number of sales she needs to make to pay her monthly bills, you can use a multi-step inequality.



**Solve Multi-Step Inequalities** Multi-step inequalities can be solved by undoing the operations in the same way you would solve a multi-step equation.

### 🕙 Real-World EXAMPLE 1

### Solve a Multi-Step Inequality

**SALES** Write and solve an inequality to find the sales Mrs. Jones needs if she earns a monthly salary of \$2000 plus a 10% commission on her sales. Her goal is to make at least \$4000 per month. What sales does she need to meet her goal?

base salary + (commission  $\times$  sales)  $\geq$  income needed

$$2000 + 0.10x \ge 4000$$

Substitution

 $0.10x \ge 2000$ 

Subtract 2000 from each side.

 $x \ge 20,000$ 

Divide each side by 0.10.

She must make at least \$20,000 in sales to meet her monthly goal.



### **Check Your Progress**

**1. FINANCIAL LITERACY** The Print Shop advertises a special to print 400 flyers for less than the competition. The price includes a \$3.50 set-up fee. If the competition charges \$35.50, what does the Print Shop charge for each flyer?



When multiplying or dividing by a negative number, the direction of the inequality symbol changes. This holds true for multi-step inequalities.

### **EXAMPLE 2** Inequality Involving a Negative Coefficient

Solve 
$$-11y - 13 > 42$$
.

$$-11y - 13 > 42$$
 Original inequality

$$-11y > 55$$
 Add 13 to each side and simplify.

$$\frac{-11y}{-11} < \frac{55}{-11}$$
 Divide each side by -11, and reverse the inequality.

$$y < -5$$
 Simplify.

The solution set is  $\{y|y<-5\}$ .



**Check Your Progress** Solve each inequality.

**2A.** 
$$23 \ge 10 - 2w$$

**2B.** 
$$43 > -4y + 11$$

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You can translate sentences into multi-step inequalities and then solve them using the Properties of Inequalities.

Math in Motion, **Interactive Lab** glencoe.com

#### **EXAMPLE 3** Write and Solve an Inequality

Define a variable, write an inequality, and solve the problem.

Five minus 6 times a number is more than four times the number plus 45. Let n be the number.

Five	minus	six times a number	is more	four times a number	plus	forty-five.
5	_ 6	6n	>	4n	+	45
5 - 10n > 45	Su	ıbtract 4 <i>n</i> from	each side and	simplify.		
-10n > 40	Su	ıbtract 5 from ea	ach side and	simplify.		
$\frac{-10n}{-10} < \frac{40}{-10}$	Di	vide each side b	y —10, and ı	reverse the ine	quality.	
n < -4	Si	mplify.				

The solution set is  $\{n \mid n < -4\}$ .



#### order of operations

- 1. Evaluate expressions inside grouping symbols.
- 2. Evaluate all powers.
- 3. Multiply and/or divide from left to right.
- 4. Add and/or subtract from left to right. (Lesson 1-2)

### Check Your Progress

**3.** Two more than half of a number is greater than twenty-seven.

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Solve Inequalities Involving the Distributive Property When solving inequalities that contain grouping symbols, use the Distributive Property to remove the grouping symbols first. Then use the order of operations to simplify the resulting inequality.

#### **EXAMPLE 4 Distributive Property**

Solve 
$$4(3t-5)+7\geq 8t+3$$
.  
 $4(3t-5)+7\geq 8t+3$  Original inequality  
 $12t-20+7\geq 8t+3$  Distributive Property  
 $12t-13\geq 8t+3$  Combine like terms.  
 $4t-13\geq 3$  Subtract 8t from each side and simplify.  
 $4t\geq 16$  Add 13 to each side.  
 $\frac{4t}{4}\geq \frac{16}{4}$  Divide each side by 4.  
 $t\geq 4$  Simplify.

The solution set is  $\{t \mid t \geq 4\}$ .

#### Watch Out!

#### **Distributive Property**

If a negative number is multiplied by a sum or difference, remember to distribute the negative sign along with the number to each term inside the parentheses.

### Check Your Progress

Solve each inequality. Check your solution.

**4A.** 
$$6(5z - 3) \le 36z$$

**4B.** 
$$2(h+6) > -3(8-h)$$

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If solving an inequality results in a statement that is always true, the solution set is the set of all real numbers. This solution set is written as  $\{x \mid x \text{ is a real number.}\}$ . If solving an inequality results in a statement that is never true, the solution set is the empty set, which is written as the symbol Ø. The empty set has no members.

### StudyTip

**Empty Set** Set-builder notation is not required when the solution set is the empty set. Instead, the solution is written as the symbol  $\varnothing$ .

#### EXAMPLE 5 **Empty Set and All Reals**

Solve each inequality. Check your solution.

**a.** 
$$9t - 5(t - 5) \le 4(t - 3)$$

$$9t - 5(t - 5) \le 4(t - 3)$$

$$9t - 5t + 25 \le 4t - 12$$

$$4t + 25 \le 4t - 12$$

$$4t + 25 - 4t \le 4t - 12 - 4t$$

$$25 \le -12$$

Since the inequality results in a false statement, the solution set is the empty set, Ø.

**b.** 
$$3(4m+6) \le 42 + 6(2m-4)$$

$$3(4m+6) \le 42 + 6(2m-4)$$

$$12m + 18 \le 42 + 12m - 24$$

**Distributive Property** 

$$12m + 18 \le 12m + 18$$

Combine like terms.

Subtract 12m from each side.

$$12m + 18 - 12m \le 12m + 18 - 12m$$

Simplify.

$$18 \le 18$$
 Sin

All values of *m* make the inequality true. All real numbers are solutions.



Solve each inequality. Check your solution.

**5A.** 
$$18 - 3(8c + 4) \ge -6(4c - 1)$$

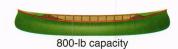
**5B.** 
$$46 \le 8m - 4(2m + 5)$$

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## Check Your Understanding

#### **Example 1** p. 296

1. **CANOEING** If four people plan to use the canoe with 60 pounds of supplies, write and solve an inequality to find the allowable average weight per person.



**2. SHOPPING** Rita is ordering a movie for \$11.95 and a few CDs. She has \$50 to spend. Shipping and sales tax will be \$10. If each CD costs \$9.99, write and solve an inequality to find the greatest number of CDs that she can buy.

#### **Example 2** Solve each inequality. Check your solution.

p. 296

$$6h - 10 ≥ 32$$

**4.** 
$$-3 \le \frac{2}{3}r + 9$$

**5.** 
$$-3x + 7 > 43$$

**6.** 
$$4m - 17 < 6m + 25$$

#### Example 3 Define a variable, write an inequality, and solve each problem. Then check your p. 297 solution.

- **7.** Four times a number minus 6 is greater than eight plus two times the number.
- **8.** Negative three times a number plus 4 is less than five times the number plus 8.

#### **Examples 4 and 5** pp. 297-298

Solve each inequality. Check your solution.

**9.** 
$$-6 < 3(5v - 2)$$

**9.** 
$$-6 \le 3(5v - 2)$$
 **10.**  $-5(g + 4) > 3(g - 4)$  **11.**  $3 - 8x \ge 9 + 2(1 - 4x)$ 

11. 
$$3 - 8x \ge 9 + 2(1 - 4x)$$

#### **Examples 1 and 2** p. 296

Solve each inequality. Check your solution.

**12.** 
$$5b - 1 \ge -11$$

12. 
$$50 - 1 \ge -11$$
14.  $-9 \ge \frac{2}{5}m + 7$ 

**16.** 
$$-a + 6 \le 5$$

**18.** 
$$8 - \frac{z}{3} \ge 11$$

**20.** 
$$3b - 6 \ge 15 + 24b$$

$$13$$
 21 > 15 + 2a

**15.** 
$$\frac{w}{8} - 13 > -6$$

17. 
$$37 < 7 - 10w$$

**19.** 
$$-\frac{5}{4}p + 6 < 12$$

**21.** 
$$15h + 30 < 10h - 45$$

#### **Example 3** p. 297

Define a variable, write an inequality, and solve each problem. Check your solution.

- 22. Three fourths of a number decreased by nine is at least forty-two.
- **23.** Two thirds of a number added to six is at least twenty-two.
- **24.** Seven tenths of a number plus 14 is less than forty-nine.
- 25. Eight times a number minus twenty-seven is no more than the negative of that number plus eighteen.
- 26. Ten is no more than 4 times the sum of twice a number and three.
- 27. Three times the sum of a number and seven is greater than five times the number less thirteen.
- 28. The sum of nine times a number and fifteen is less than or equal to the sum of twenty-four and ten times the number.

**Examples 4 and 5** 





#### Real-World Career

#### Veterinarian

Veterinarians take care of sick and injured animals. Vets can work anywhere from a zoo to a research facility to owning their own practice. Vets need to earn a bachelor's degree, attend vet college for 4 years, and take a test to get licensed.

Solve each inequality. Check your solution.

**29.** 
$$-3(7n+3) < 6n$$

**31.** 
$$2y + 4 > 2(3 + y)$$

**33.** 
$$7 + t \le 2(t + 3) + 2$$

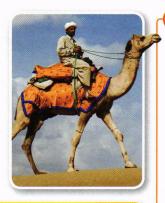
**30.** 
$$21 \ge 3(a-7) + 9$$

**32.** 
$$3(2-b) < 10 - 3(b-6)$$

**34.** 
$$8a + 2(1 - 5a) \le 20$$

Define a variable, write an inequality, and solve each problem. Then interpret your solution.

- **35.** CARS A car salesperson is paid a base salary of \$35,000 a year plus 8% of sales. What are the sales needed to have an annual income greater than \$65,000?
- **36. ANIMALS** Keith's dog weighs 90 pounds. A healthy weight for his dog would be less than 75 pounds. If Keith's dog can lose an average of 1.25 pounds per week on a certain diet, how long until the dog reaches a healthy weight?
- **37.** Solve 6(m-3) > 5(2m+4). Show each step and justify your work.
- **38.** Solve  $8(a-2) \le 10(a+2)$ . Show each step and justify your work.
- **39.** MUSICAL A high school drama club is performing a musical to benefit a local charity. Tickets are \$5 each. They also received donations of \$565. They want to raise at least \$1500.
  - **a.** Write an inequality that describes this situation. Then solve the inequality.
  - **b.** Graph the solution.
- **40. ICE CREAM** Benito has \$6 to spend. A sundae costs \$3.25 plus \$0.65 per topping. Write and solve an inequality to find how many toppings he can order.



#### Real-World Link

Unlike most animals, camels move both legs on one side of their body at the same time as they walk.

Source: National Zoo

- **SCIENCE** The normal body temperature of a camel is 97.7°F in the morning. If it has had no water by noon, its body temperature can be greater than 104°F.
  - **a.** Write an inequality that represents a camel's body temperature at noon if the camel had no water.
  - **b.** If C represents degrees Celsius, then  $F = \frac{9}{5}C + 32$ . Write and solve an inequality to find the camel's body temperature at noon in degrees Celsius.
- **42. NUMBER THEORY** Find all sets of three consecutive positive even integers with a sum no greater than 36.
- **43. NUMBER THEORY** Find all sets of four consecutive positive odd integers whose sum is less than 42.

Solve each inequality. Check your solution.

**44.** 
$$2(x-4) \le 2 + 3(x-6)$$

**45.** 
$$\frac{2x-4}{6} \ge -5x+2$$

**46.** 
$$5.6z + 1.5 < 2.5z - 4.7$$

**47.** 
$$0.7(2m-5) \ge 21.7$$

**GRAPHING CALCULATOR** Use a graphing calculator to solve each inequality.

**48.** 
$$3x + 7 > 4x + 9$$

**49.** 
$$13x - 11 \le 7x + 37$$

**48.** 
$$3x + 7 > 4x + 9$$
 **49.**  $13x - 11 \le 7x + 37$  **50.**  $2(x - 3) < 3(2x + 2)$ 

**51.** 
$$\frac{1}{2}x - 9 < 2x$$

**52.** 
$$2x - \frac{2}{3} \ge x - 22$$

**52.** 
$$2x - \frac{2}{3} \ge x - 22$$
 **53.**  $\frac{1}{3}(4x + 3) \ge \frac{2}{3}x + 2$ 

- **54. MULTIPLE REPRESENTATIONS** In this problem, you will solve compound inequalities. A number x is greater than 4, and the same number is less than 9.
  - **a. NUMERICAL** Write two separate inequalities for the statement.
  - **b. GRAPHICAL** Graph the solution set for the first inequality in red. Graph the solution set for the second inequality in blue. Highlight the portion of the graph in which the red and blue overlap.
  - **c. TABULAR** Make a table using ten points from your number line, including points from each section. Use one column for each inequality and a third column titled "Both are True." Complete the table by writing true or false.
  - **d. VERBAL** Describe the relationship between the colored regions of the graph and the chart.
  - **e. LOGICAL** Make a prediction of what the graph of 4 < x < 9 looks like.

#### **H.O.T. Problems**

Use Higher-Order Thinking Skills

- **55. REASONING** Explain how you could solve  $-3p + 7 \ge -2$  without multiplying or dividing each side by a negative number.
- **56.** CHALLENGE If ax + b < ax + c has infinitely many solutions, what will be the solution of ax + b > ax + c? Explain how you know.
- **57. OPEN ENDED** Write two different multi-step inequalities that have the same graph.
- **58.** WHICH ONE DOESN'T BELONG? Name the inequality that does not belong. Explain.

$$4y + 9 > -3$$

$$3y - 4 > 5$$

$$-2y + 1 < -5$$

$$-5y + 2 < -13$$

**59. WRITING IN MATH** Explain when the solution set of an inequality will be the empty set or the set of all real numbers. Show an example of each.

### **Standardized Test Practice**

**60.** What is the solution set of the inequality 4t + 2 < 8t - (6t - 10)?

**A** 
$$\{t \mid t < -6.5\}$$

**C** 
$$\{t \mid t < 4\}$$

**B** 
$$\{t \mid t > -6.5\}$$

**D** 
$$\{t \mid t > 4\}$$

**61. GEOMETRY** The section of Liberty Ave. between 5th St. and King Ave. is temporarily closed. Traffic is being detoured right on 5th St., left on King Ave. and then back on Liberty Ave. How long is the closed section of Liberty Ave.?



- **62. SHORT RESPONSE** Rhiannon is paid \$52 for working 4 hours. At this rate, how many hours will it take her to earn \$845?
- **63. GEOMETRY** Classify the triangle.



- A right
- **B** parallel
- C obtuse
- **D** equilateral

### **Spiral Review**

Solve each inequality. Check your solution. (Lesson 5-2)

**64.** 
$$\frac{y}{2} \le -5$$

**65.** 
$$12b > -48$$

**66.** 
$$-\frac{2}{3}t \le -30$$

Solve each inequality. Check your solution, and graph it on a number line. (Lesson 5-1)

**67.** 
$$6 - h > -8$$

**68.** 
$$p - 9 < 2$$

**69.** 
$$3 \ge 4 - m$$

Solve each equation by graphing. Verify your answer algebraically. (Lesson 3-2)

**70.** 
$$2x - 7 = 4x + 9$$

**71.** 
$$5 + 3x = 7x - 11$$

**72.** 
$$2(x-3) = 5x + 12$$

73. THEME PARKS In 2006, attendance at the top 20 theme parks in North America was 119.8 million. That represents an increase of about 1.5% from 2005. What was the approximate attendance in 2005? (Lesson 2-7)

If f(x) = 4x - 3 and  $g(x) = 2x^2 + 5$ , find each value. (Lesson 1-7)

**74.** 
$$f(-2)$$

**75.** 
$$g(2) - 5$$

**76.** 
$$f(c+3)$$

77. **COSMETOLOGY** On average, a barber received a tip of \$4 for each of 12 haircuts. Write and evaluate an expression to determine the total amount that she earned. (Lesson 1-4)



### **Skills Review**

Graph each set of numbers on a number line.

**78.** 
$$\{-4, -2, 2, 4\}$$

**82.** {integers between 
$$-3$$
 and  $4$ }

**81.** {integers greater than or equal to 
$$-2$$
}

**83.** {integers less than 
$$-1$$
}

Solve each inequality. Then graph it on a number line. (Lesson 5-1)

1. 
$$x - 8 > 4$$

**2.** 
$$m + 2 \ge 6$$

3. 
$$p-4 < -7$$

**4.** 
$$12 \le t - 9$$

- **5. CONCERTS** Lupe's allowance for the month is \$60. She wants to go to a concert for which a ticket costs \$45. (Lesson 5-1)
  - **a.** Write and solve an inequality that shows how much money she can spend that month after buying a concert ticket.
  - **b.** She spends \$9.99 on music downloads and \$2 on lunch in the cafeteria. Write and solve an inequality that shows how much she can spend after these purchases and the concert ticket.

Define a variable, write an inequality, and solve each problem. Check your solution. (Lesson 5-2)

- **6.** The sum of a number and -2 is no more than 6.
- **7.** A number decreased by 4 is more than -1.
- **8.** Twice a number increased by 3 is less than the number decreased by 4.
- **9. MULTIPLE CHOICE** Jane is saving money to buy a new cell phone that costs no more than \$90. So far, she has saved \$52. How much more money does Jane need to save? (Lesson 5-2)
  - A \$38
  - B more than \$38
  - C no more than \$38
  - D at least \$38

Solve each inequality. Check your solution. (Lesson 5-2)

**10.** 
$$\frac{1}{3}y \ge 5$$

11. 
$$4 < \frac{c}{5}$$

12. 
$$-8x > 24$$

**13.** 
$$2m \le -10$$

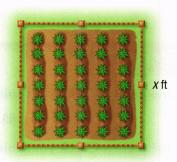
**14.** 
$$\frac{x}{2} < \frac{5}{8}$$

**15.** 
$$-9a \ge -45$$

**16.** 
$$\frac{w}{6} > -3$$

17. 
$$\frac{k}{7} < -2$$

- **18. ANIMALS** The world's heaviest flying bird is the great bustard. A male bustard can be up to 4 feet long and weigh up to 40 pounds. (Lesson 5-2)
  - **a.** Write inequalities to describe the ranges of lengths and weights of male bustards.
  - **b.** Male bustards are usually about four times as heavy as females. Write and solve an inequality that describes the range of weights of female bustards.
- **19. GARDENING** Bill is building a fence around a square garden to keep deer out. He has 60 feet of fencing. Find the maximum length of a side of the garden. (Lesson 5-3)



Solve each inequality. Check your solution. (Lesson 5-3)

**20.** 
$$4a - 2 > 14$$

**21.** 
$$2x + 11 \le 5x - 10$$

**22.** 
$$-p + 4 < -9$$

**23.** 
$$\frac{d}{4} + 1 \ge -3$$

**24.** 
$$-2(4b+1) < -3b+8$$

Define a variable, write an inequality, and solve each problem. Check your solution. (Lesson 5-3)

- **25.** Three times a number increased by 8 is no more than the number decreased by 4.
- **26.** Two thirds of a number plus 5 is greater than 17.
- **27. MULTIPLE CHOICE** Shoe rental costs \$2, and each game bowled costs \$3. How many games can Kyle bowl without spending more than \$15? (Lesson 5-3)

$$J = 5$$

## **Reading Compound Statements**

A compound statement is made up of two simple statements connected by the word and or or. Before you can determine whether a compound statement is true or false, you must understand what the words and and or mean.

#### A spider has eight legs, and a dog has five legs.

For a compound statement connected by the word and to be true, both simple statements must be true.



A spider has eight legs. → true



A dog has five legs.  $\rightarrow$  false

Since one of the statements is false, the compound statement is false.

A compound statement connected by the word or may be exclusive or inclusive. For example, the statement "With your lunch, you may have milk or juice," is exclusive. In everyday language, or means one or the other, but not both. However, in mathematics, or is inclusive. It means one or the other or both.

### A spider has eight legs, or a dog has five legs.

For a compound statement connected by the word or to be true, at least one of the simple statements must be true. Since it is true that a spider has eight legs, the compound statement is true.

#### **Exercises**

Is each compound statement true or false? Explain.

- 1. Most top 20 movies in 2004 were rated PG-13, or most top 20 movies in 2002 were rated G.
- 2. In 2005 more top 20 movies were rated PG than were rated G, and more were rated PG than rated PG-13.
- **3.** For the years shown most top 20 movies are rated PG-13, and no top 20 movies in 2002 were rated R.
- **4.** No top 20 movies in 2005 were rated *G*, *or* most top 20 movies in 2005 were not rated PG.

**5.** 
$$11 < 5$$
 or  $9 < 7$ 

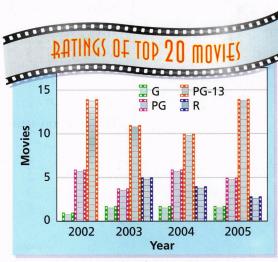
**6.** 
$$-2 > 0$$
 and  $3 < 7$ 

7. 
$$5 > 0$$
 and  $-3 < 0$ 

8. 
$$-2 > -3$$
 or  $0 = 0$ 

**9.** 
$$8 \neq 8$$
 or  $-2 > -5$ 

**10.** 
$$5 > 10$$
 and  $4 > -2$ 



Source: National Association of Theater Owners

### Then

You solved absolute value equations with two cases. (Lesson 2-5)

#### Now

- Solve compound inequalities containing the word and, and graph their solution set.
- Solve compound inequalities containing the word or, and graph their solution set.

### New Vocabulary

compound inequality intersection union

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## **Solving Compound Inequalities**

To ride the Mind Eraser roller coaster at Six Flags in Baltimore, Maryland, you must be at least 52 inches tall, and your height cannot exceed 72 inches. If h represents the height of a rider, we can write two inequalities to represent this.

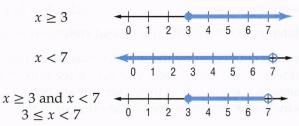
at least 52 inches cannot exceed 72 inches 
$$h > 52$$
  $h < 72$ 

The inequalities  $h \ge 52$  and  $h \le 72$  can be combined and written without using and as  $52 \le h \le 72$ .



**Inequalities Containing and** When considered together, two inequalities such as  $h \ge 52$  and  $h \le 72$  form a compound inequality. A compound inequality containing and is only true if both inequalities are true. Its graph is where the graphs of the two inequalities overlap. This is called the intersection of the two graphs.

The intersection can be found by graphing each inequality and then determining where the graphs intersect.



The statement  $3 \le x < 7$  can be read as x is greater than or equal to 3 and less than 7 or x is between 3 and 7 including 3.

### **EXAMPLE 1** Solve and Graph an Intersection

Solve  $-2 \le x - 3 < 4$ . Then graph the solution set.

First, express  $-2 \le x - 3 < 4$  using and. Then solve each inequality.

$$-2 \le x - 3$$

and 
$$x - 3 < 4$$

Write the inequalities.

$$-2 + 3 \le x - 3 + 3$$

x - 3 + 3 < 4 + 3

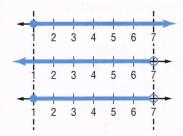
Add 3 to each side.

 $1 \leq x$ 

x < 7

Simplify.

The solution set is  $\{x \mid 1 \le x < 7\}$ . Now graph the solution set.



Graph  $1 \le x$  or  $x \ge 1$ .

Graph x < 7.

Find the intersection of the graphs.



### **Check Your Progress**

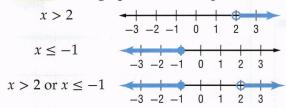
Solve each compound inequality. Then graph the solution set.

**1A.** 
$$y - 3 \ge -11$$
 and  $y - 3 \le -8$ 

**1B.** 
$$6 \le r + 7 < 10$$

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**Inequalities Containing or** Another type of compound inequality contains the word or. A compound inequality containing or is true if at least one of the inequalities is true. Its graph is the **union** of the graphs of two inequalities.



When solving problems involving inequalities, within is meant to be inclusive, so use  $\geq$  or  $\leq$ . Between is meant to be exclusive, so use < or >.

### ReadingMath

At Most The phrase at most in Example 2 indicates  $\leq$  . It could also have been phrased as *no more* than or less than or equal to.

Math in Motion, **Animation glencoe.com** 

#### Real-World EXAMPLE 2

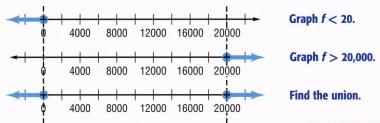
### Write and Graph a Compound Inequality

**SOUND** The human ear can only detect sounds between the frequencies 20 Hertz and 20,000 Hertz. Write and graph a compound inequality that describes the frequency of sounds humans cannot hear.

The problem states that humans can hear the frequencies between 20 Hz and 20,000 Hz. We are asked to find the frequencies humans cannot hear.

Words	The frequency	is at most	20 Hertz	or	The frequency	is at least	20,000 Hertz.
Variable	Let f be the frequ	uency.					
Inequality	f	$\leq$	20	or	<b>f</b>	≥	20,000

Now, graph the solution set.



Notice that the graphs do not intersect. Humans cannot hear sounds at a frequency less than 20 Hertz or greater than 20,000 Hertz. The compound inequality is  $\{f | f < 20 \text{ or } f > 20,000\}$ .

### **Check Your Progress**

**2. MANUFACTURING** A company is manufacturing an action figure that must be at least 11.2 centimeters and at most 11.4 centimeters tall. Write and graph a compound inequality that describes how tall the action figure can be.

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#### **EXAMPLE 3**

#### **Solve and Graph a Union**

Solve  $-2m + 7 \le 13$  or 5m + 12 > 37. Then graph the solution set.

$$-2m + 7 \le 13$$

or

$$5m + 12 > 37$$

$$-2m + 7 - 7 \le 13 - 7$$

Subtract.

$$5m + 12 - 12 > 37 - 12$$

$$-2m < 6$$

Simplify.

$$-2m \le 6$$

5m > 25

$$\frac{-2m}{-2} \ge \frac{6}{-2}$$

Divide.

 $\frac{5m}{5} > \frac{25}{5}$ 

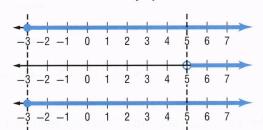
$$m \ge -3$$

Simplify.

Graph  $m \ge -3$ .

Graph m > 5.

Find the union.



Notice that the graph of  $m \ge -3$  contains every point in the graph of m > 5. So, the union is the graph of  $m \ge -3$ . The solution set is  $\{m \mid m \ge -3\}$ .

## **StudyTip**

Intersections and **Unions** The graphs of compound inequalities containing and will be an intersection. The graphs of compound inequalities containing or will be a union.

### **Check Your Progress**

Solve each compound inequality. Then graph the solution set.

**3A.** 
$$a + 1 < 4$$
 or  $a - 1 \ge 3$ 

**3B.** 
$$x \le 9 \text{ or } 2 + 4x < 10$$

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## Check Your Understanding

#### Examples 1 and 3 pp. 304, 306

Solve each compound inequality. Then graph the solution set.

**1.** 
$$4 \le p - 8$$
 and  $p - 14 \le 2$ 

**2.** 
$$r + 6 < -8 \text{ or } r - 3 > -10$$

**3.** 
$$4a + 7 \ge 31$$
 or  $a > 5$ 

**4.** 
$$2 \le g + 4 < 7$$

#### **Example 2** p. 305

5. BIKES The recommended air pressure for the tires of a mountain bike is at least 35 pounds per square inch (psi), but no more than 80 pounds per square inch. If a bike's tires have 24 pounds per square inch, what is the recommended range of air that should be put into the tires?

### **Practice and Problem Solving**

Step-by-Step Solutions begin on page R12. Extra Practice begins on page 815.

#### Examples 1 and 3 pp. 304, 306

Solve each compound inequality. Then graph the solution set.

**6.** 
$$f - 6 < 5$$
 and  $f - 4 \ge 2$ 

$$n + 2 \le -5$$
 and  $n + 6 \ge -6$ 

**8.** 
$$y - 1 \ge 7$$
 or  $y + 3 < -1$ 

**9.** 
$$t + 14 \ge 15$$
 or  $t - 9 < -10$ 

**10.** 
$$-5 < 3p + 7 \le 22$$

11. 
$$-3 \le 7c + 4 < 18$$

**12.** 
$$5h + -4 \ge 6$$
 and  $7h + 11 < 32$ 

13. 
$$22 \ge 4m - 2$$
 or  $5 - 3m \le -13$ 

**14.** 
$$-4a + 13 \ge 29$$
 and  $10 < 6a - 14$ 

**15.** 
$$-y + 5 \ge 9 \text{ or } 3y + 4 < -5$$

Example 2 p. 305

- **16. SPEED** The posted speed limit on an interstate highway is shown. Write an inequality that represents the sign. Graph the inequality.
- 17. **NUMBER THEORY** Find all sets of two consecutive positive odd integers with a sum that is at least 8 and less than 24.

SPEED LIMIT MINIMUM

Write a compound inequality for each graph.



Solve each compound inequality. Then graph the solution set.

**24.** 
$$3b + 2 < 5b - 6 \le 2b + 9$$

**25.** 
$$-2a + 3 \ge 6a - 1 > 3a - 10$$

**26.** 
$$10m - 7 < 17m \text{ or } -6m > 36$$

**27.** 
$$5n - 1 < -16$$
 or  $-3n - 1 < 8$ 

- **28. COUPON** Juanita has a coupon for 10% off any digital camera at a local electronics store. She is looking at digital cameras that range in price from \$100 to \$250.
  - **a.** How much are the cameras after the coupon is used?
  - **b.** If the tax amount is 6.5%, how much should Juanita expect to spend?

Define a variable, write an inequality, and solve each problem. Then check your solution.

- **29.** Eight less than a number is no more than 14 and no less than 5.
- **30.** The sum of 3 times a number and 4 is between -8 and 10.
- **31.** The product of -5 and a number is greater than 35 or less than 10.
- **32.** One half a number is greater than 0 and less than or equal to 1.
- **33. SNAKES** Most snakes live where the temperature ranges from 75°F to 90°F, inclusive. Write an inequality to represent temperatures where snakes will not thrive.



- **34. FUNDRAISING** Yumas is selling gift cards to raise money for a class trip. He can earn prizes depending on how many cards he sells. So far, he has sold 34 cards. How many more does he need to sell to earn a prize in category 4?
- **35. TURTLES** Atlantic sea turtle eggs that incubate below 23°C or above 33°C rarely hatch. Write an inequality for the temperatures at which the eggs should be incubated.

Cards	Prize
1-15	1
16-30	2
31-45	3
46-60	4
+61	5

- **36. GEOMETRY** The *Triangle Inequality Theorem* states that the sum of the The organization Field measures of any two sides of a triangle is greater than the measure of Trip Earth monitors the locations of Atlantic sea the third side.
  - **a.** Write and solve three inequalities to express the relationships among the measures of the sides of the triangle shown at the right.
  - **b.** What are four possible lengths for the third side of the triangle?
  - **c.** Write a compound inequality for the possible values of x.





turtles. This data allows the scientists to track migration patterns as part of a wildlife conservation

Real-World Link

project.

Source: Field Trip Earth



#### Real-World Link

Between 2001 and 2004, a total of nine hurricanes struck the mainland United States. Of these, three were classified as Category 3, 4, or 5.

Source: National Weather Service

- **HURRICANES** The Saffir-Simpson Hurricane Scale rates hurricanes on a scale from 1 to 5 based on their wind speed.
  - **a.** Write a compound inequality for the wind speeds of a category 3 and a category 4 hurricane.
  - **b.** What is the intersection of the two graphs of the inequalities you found in part a?

Category	Wind Speed (mph)	Example (year)
1	74–95	Gaston (2004)
2	96-110	Frances (2004)
3	111–130 Ivan (200	
4	131–155 Charley (200	
5	> 155	Andrew (1992)

- **38.** WULTIPLE REPRESENTATIONS In this problem, you will investigate measurements. The absolute error of a measurement is equal to one half the unit of measure. The relative error of a measure is the ratio of the absolute error to the expected measure.
  - **a. TABULAR** Copy and complete the table.

Measure	Absolute Error	Relative Error
14.3 cm	$\frac{1}{2}(0.1) = 0.05 \text{ cm}$	$\frac{\text{absolute error}}{\text{expected measure}} = \frac{0.05 \text{ cm}}{14.3 \text{ cm}}$ $\approx 0.0035 \text{ or } 0.4\%$
1.85 cm		
61.2 cm	daily be the several to	
237 cm		

- **b. ANALYTICAL** You measured a length of 12.8 centimeters. Compute the absolute error and then write the range of possible measures.
- **c. LOGICAL** To what precision would you have to measure a length in centimeters to have an absolute error of less than 0.05 centimeter?
- **d. ANALYTICAL** To find the relative error of an area or volume calculation, add the relative errors of each linear measure. If the measures of the sides of a rectangular box are 6.5 centimeters, 7.2 centimeters, and 10.25 centimeters, what is the relative error of the volume of the box?

### **H.O.T. Problems**

Use Higher-Order Thinking Skills

**39. ERROR ANALYSIS** Chloe and Jonas are solving 3 < 2x - 5 < 7. Is either of them correct? Explain your reasoning.

Jonas
3 < 2× - 5 < 7
8 < 2× < 7
4 < × < 
$$\frac{7}{2}$$

- **40. REASONING** Write a compound inequality for which the graph is the empty set and one for which the graph is the set of all real numbers.
- **41. OPEN ENDED** Create an example of a compound inequality containing *or* that has infinitely many solutions.
- **42. CHALLENGE** Determine whether the following statement is *always*, *sometimes*, or never true. Explain. The graph of a compound inequality that involves an or statement is bounded on the left and right by two values of x.
- **43.** WRITING IN MATH Give an example of a compound inequality you might encounter at an amusement park. Does the example represent an intersection or a union?

### **Standardized Test Practice**

**44.** What is the solution set of the inequality -7 < x + 2 < 4?

**A** 
$$\{x \mid -5 < x < 6\}$$

**A** 
$$\{x \mid -5 < x < 6\}$$
 **C**  $\{x \mid -9 < x < 2\}$ 

**B** 
$$\{x \mid -5 < x < 2\}$$
 **D**  $\{x \mid -9 < x < 6\}$ 

**D** 
$$\{x \mid -9 < x < 6\}$$

**45. GEOMETRY** What is the surface area of the rectangular solid?

$$G 278.4 \text{ cm}^2$$



**46. GRIDDED RESPONSE** What is the next term in the sequence?

$$\frac{13}{2}$$
,  $\frac{18}{5}$ ,  $\frac{23}{8}$ ,  $\frac{28}{11}$ ,  $\frac{33}{14}$ , ...

47. After paying a \$15 membership fee, members of a video club can rent movies for \$2. Nonmembers can rent movies for \$4. What is the least number of movies which must be rented for it to be less expensive for members?

### **Spiral Review**

- 48. BABYSITTING Marilyn earns \$150 per month delivering newspapers plus \$7 an hour babysitting. If she wants to earn at least \$300 this month, how many hours will she have to babysit? (Lesson 5-3)
- **49.** MAGAZINES Carlos has earned more than \$260 selling magazine subscriptions. Each subscription was sold for \$12. How many did Carlos sell? (Lesson 5-2)
- **50. PUNCH** Raquel is mixing lemon-lime soda and a fruit juice blend that is 45% juice. If she uses 3 quarts of soda, how many quarts of fruit juice must be added to produce punch that is 30% juice? (Lesson 2-9)

Solve each proportion. If necessary, round to the nearest hundredth. (Lesson 2-6)

**51.** 
$$\frac{14}{x} = \frac{20}{8}$$

**52.** 
$$\frac{0.47}{6} = \frac{1.41}{m}$$

**53.** 
$$\frac{16}{7} = \frac{9}{b}$$

**54.** 
$$\frac{2+y}{5} = \frac{10}{3}$$

**55.** 
$$\frac{8}{9} = \frac{2r-3}{4}$$

**56.** 
$$\frac{6-2y}{8} = \frac{2}{18}$$

Determine whether a valid conclusion follows from the statement below for each given condition. If a valid conclusion does not follow, write no valid conclusion and explain why. (Lesson 1-8)

If a DVD box set costs less than \$70, then Ian will buy one.

**57.** A DVD box set costs \$59.

**58.** A DVD box set costs \$89.

**59.** Ian will not buy a DVD box set.

**60.** Ian bought 2 DVD box sets.

Evaluate each expression. Name the property used in each step. (Lesson 1-2)

**61.** 
$$5 + (4 - 2^2)$$

**62.** 
$$\frac{3}{8}[8 \div (7-4)]$$

**63.** 
$$2(4 \cdot 9 - 3) + 5 \cdot \frac{1}{5}$$

### Skills Review

Solve each equation. (Lesson 2-3)

**64.** 
$$4p - 2 = -6$$

**65.** 
$$18 = 5p + 3$$

**66.** 
$$9 = 1 + \frac{m}{7}$$

**67.** 
$$1.5a - 8 = 11$$

**68.** 
$$20 = -4c - 8$$

**66.** 
$$9 = 1 + \frac{m}{7}$$
  
**69.**  $\frac{b+4}{-2} = -17$ 

**70.** 
$$\frac{n-3}{8} = 20$$

**71.** 
$$6y - 16 = 44$$

**72.** 
$$130 = 11k + 9$$

#### Then

You solved equations involving absolute value. (Lesson 2-5)

#### Now

- Solve and graph absolute value inequalities (<).
- Solve and graph absolute value inequalities (>).

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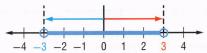
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## **Inequalities Involving Absolute Value**

### Why?

Some companies use absolute value inequalities to control the quality of their product. To make baby carrots, long carrots are sliced into 3-inch sections and peeled. If the machine is accurate to within  $\frac{1}{8}$  of an inch, the length ranges from  $2\frac{7}{8}$  inches to  $3\frac{1}{8}$  inches.

**Absolute Value Inequalities (<)** The inequality |x| < 3 means that the distance between x and 0 is less than 3.





So, x > -3 and x < 3. The solution set is  $\{x \mid -3 < x < 3\}$ .

When solving absolute value inequalities, there are two cases to consider.

**Case 1** The expression inside the absolute value symbols is nonnegative.

**Case 2** The expression inside the absolute value symbols is negative.

The solution is the intersection of the solutions of these two cases.

### **EXAMPLE 1** Solve Absolute Value Inequalities (<)

Solve each inequality. Then graph the solution set.

a. 
$$|m+2| < 11$$

Rewrite |m + 2| < 11 for Case 1 and Case 2.

Case 1 m + 2 is nonnegative. and

$$m + 2 < 11$$

$$m + 2 - 2 < 11 - 2$$

m < 9

Case 2 
$$m + 2$$
 is negative.

$$-(m+2) < 11$$

$$m + 2 > -11$$

$$m + 2 - 2 > -11 - 2$$

$$m > -13$$

So, m < 9 and m > -13. The solution set is  $\{m \mid -13 < m < 9\}$ .



**b.** 
$$|y-1| < -2$$

|y-1| cannot be negative. So it is not possible for |y-1| to be less than -2. Therefore, there is no solution, and the solution set is the empty set,  $\emptyset$ .

### **Check Your Progress**

**1A.** 
$$|n-8| \le 2$$

**1B.** 
$$|2c - 5| < -3$$

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#### Real-World Link

One in five Americans use the Internet to view videos. Young adults tend to watch funny videos, while other age groups tend to watch the news.

**Source:** Pew Internet and American Life Project

### Real-World EXAMPLE 2 Apply Absolute Value Inequalities

**INTERNET** A recent survey showed that 65% of young adults watched online video clips. The margin of error was within 3 percentage points. Find the range of young adults who use video sharing sites.

The difference between the actual number of viewers and the number from the survey is less than or equal to 3. Let x be the actual number of viewers. Then  $|x - 65| \le 3$ .

Solve each case of the inequality.

**Case 1** 
$$x - 65$$
 is nonnegative.

$$\begin{aligned}
 x - 65 &\leq 3 \\
 x - 65 + 65 &\leq 3 + 65
 \end{aligned}$$

$$65 \le 3 + 65$$
$$x \le 68$$

and Case 2 x - 65 is negative.

$$-(x - 65) \le 3$$
$$x - 65 \ge -3$$

$$x \ge 62$$

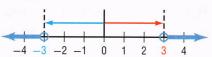
The range of young adults who use video sharing sites is  $\{x \mid 62 \le x \le 68\}$ .

### Check Your Progress

**2. CHEMISTRY** The melting point of ice is 0°C. During a chemistry experiment, Jill observed ice melting within 2°C of this measurement. Write the range of temperatures that Jill observed.

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**Absolute Value Inequalities (>)** The inequality |x| > 3 means that the distance between x and 0 is greater than 3.



So, x < -3 or x > 3. The solution set is  $\{x \mid x < -3 \text{ or } x > 3\}$ .

As in the previous example, we must consider both cases.

Case 1 The expression inside the absolute value symbols is nonnegative.

Case 2 The expression inside the absolute value symbols is negative.

### StudyTip

**Absolute Value** For  $|a| \ge b$ , where a is any linear expression in one variable and b is a negative number, the solution set will always be the set of all real numbers. Since |a| is always greater than or equal to zero, |a| is always greater than or equal to b.

### **EXAMPLE 3** Solve Absolute Value Inequalities (>)

Solve  $|3n + 6| \ge 12$ . Then graph the solution set.

Rewrite  $|3n + 6| \ge 12$  for Case 1 or Case 2.

**Case 1** 
$$3n + 6$$
 is nonnegative.

$$3n + 6 \ge 12$$
  
 $3n + 6 - 6 \ge 12 - 6$   
 $3n \ge 6$ 

$$n \ge 2$$

or

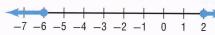
Case 2 
$$3n + 6$$
 is negative.

$$-(3n+6) \ge 12$$

$$3n + 6 \le -12$$

$$3n \le -18$$
$$n \le -6$$

So, 
$$n \ge 2$$
 or  $n \le -6$ . The solution set is  $\{n \mid n \ge 2 \text{ or } n \le -6\}$ .



### Check Your Progress

Solve each inequality. Then graph the solution set.

**3A.** 
$$|2k+1| > 7$$

**3B.** 
$$|r-6| \ge -5$$

### **Check Your Understanding**

#### **Examples 1 and 3** pp. 310-311

Solve each inequality. Then graph the solution set.

1. 
$$|a-5| < 3$$

**2.** 
$$|u+3| < 7$$

**2.** 
$$|u+3| < 7$$
 **3.**  $|t+4| \le -2$ 

**4.** 
$$|c+2| > -2$$

**5.** 
$$|n+5| \ge 3$$

**5.** 
$$|n+5| \ge 3$$
 **6.**  $|p-2| \ge 8$ 

#### Example 2 p. 311

7. FINANCIAL LITERACY Jerome bought stock in his favorite fast-food restaurant chain at \$70.85. However, it has fluctuated up to \$0.75 in a day. Find the range of prices for which the stock could trade in a day.

### Practice and Problem Solving



#### Examples 1 and 3 pp. 310-311

Solve each inequality. Then graph the solution set.

**8.** 
$$|x + 8| < 16$$

9 
$$|r+1| \le 2$$
 10.  $|2c-1| \le 7$ 

10. 
$$|2c-1| \le 7$$

**11.** 
$$|3h - 3| < 12$$

12. 
$$|m+4| < -2$$

**12.** 
$$|m+4| < -2$$
 **13.**  $|w+5| < -8$ 

**14.** 
$$|r+2| > 6$$

**15.** 
$$|k-4| > 3$$

**16.** 
$$|2h-3| \ge 9$$

**17.** 
$$|4p + 2| \ge 10$$

**18.** 
$$|5v + 3| > -9$$

**19.** 
$$|-2c-3| > -4$$

#### **Example 2** p. 311

20. SCUBA DIVING The pressure of a scuba tank should be within 500 pounds per square inch (psi) of 2500 psi. Write the range of optimum pressures.

Solve each inequality. Then graph the solution set.

**21.** 
$$|4n+3| \ge 18$$

**22.** 
$$|5t - 2| \le 6$$

**23.** 
$$\left| \frac{3h+1}{2} \right| < 8$$

**24.** 
$$\left| \frac{2p-8}{4} \right| \ge 9$$

**25.** 
$$\left| \frac{7c+3}{2} \right| \le -5$$

**25.** 
$$\left| \frac{7c+3}{2} \right| \le -5$$
 **26.**  $\left| \frac{2g+3}{2} \right| > -7$ 

**27.** 
$$|-6r-4| < 8$$

**28.** 
$$|-3p-7| > 5$$

**28.** 
$$|-3p-7| > 5$$
 **29.**  $|-h+1.5| < 3$ 

30. MUSIC DOWNLOADS Kareem is allowed to download \$10 worth of music each month. This month he has spent within \$3 of his allowance.

a. What is the range of money he has spent on music downloads this month?

**b.** Graph the range of the money that he spent.

31. CHEMISTRY Water can be present in our atmosphere as a solid, liquid, or gas. Water freezes at 32°F and vaporizes at 212°F.

a. Write the range of temperatures in which water is not a liquid.

**b.** Graph this range.

**c.** Write the absolute value inequality that describes this situation.

Write an open sentence involving absolute value for each graph.





#### Real-World Link

In the 1930s, there were about 20,000 miniature golf courses in the United States. Today there are about 4000 courses.

Source: Professional Miniature Golf Association

- **36. ANIMALS** A sheep's normal body temperature is 39°C. However, a healthy sheep may have body temperatures 1°C above or below this temperature. What is the range of body temperatures for a sheep?
- **MINIATURE GOLF** Ginger's score was within 5 strokes of her average score of 52. Determine the range of scores for Ginger's game.

Express each statement using an inequality involving absolute value. Do not solve.

- **38.** The pH of a swimming pool must be within 0.3 of a pH of 7.5.
- **39.** The temperature inside a refrigerator should be within 1.5 degrees of 38°F.
- **40.** Ramona's bowling score was within 6 points of her average score of 98.
- 41. The cruise control of a car should keep the speed within 3 miles per hour of 55.
- MULTIPLE REPRESENTATIONS In this problem, you will investigate the graphs of absolute value inequalities on a coordinate plane.
  - **a. TABULAR** Copy and complete the table. Substitute the x and f(x) values for each point into each inequality. Mark whether the resulting statement is *true* or *false*.

Point	$f(x) \geq  x-1 $	true/false	$f(x) \leq  x-1 $	true/false
(-4, 2)	A			
(-2, 2)	8			
(0, 2)	2	100		
(2, 2)	K 1			
(4, 2)	C			

- **b. GRAPHICAL** Graph f(x) = |x 1|.
- **c. GRAPHICAL** Plot each point that made  $f(x) \ge |x 1|$  a true statement on the graph in red. Plot each point that made  $f(x) \le |x - 1|$  on the graph in blue.
- **d. LOGICAL** Make a conjecture about what the graphs of  $f(x) \ge |x-1|$  and  $f(x) \le |x-1|$  look like. Complete the table with other points to verify your conjecture.
- **e. GRAPHICAL** Use what you discovered to graph  $f(x) \ge |x 3|$ .

### **H.O.T. Problems**

Use Higher-Order Thinking Skills

**43. FIND THE ERROR** Lucita sketched a graph of her solution to |2a - 3| > 1. Is she correct? Explain your reasoning.



- **44. REASONING** The graph of an absolute value inequality is sometimes, always, or never the union of two graphs. Explain.
- **45. CHALLENGE** Demonstrate why the solution of |t| > 0 is not all real numbers. Explain your reasoning.
- **46. OPEN ENDED** Write an absolute value inequality to represent a real-world situation. Interpret the solution.
- **47. WRITING IN MATH** Explain how to determine whether an absolute value inequality uses a compound inequality with and or a compound inequality with or. Then summarize how to solve absolute value inequalities.

### **Standardized Test Practice**

**48.** The formula for acceleration in a circle is  $a = \frac{v^2}{r}$ . Which of the following shows the equation solved for r?

$$\mathbf{A} \quad r = av$$

$$\mathbf{C} \quad r = av^2$$

$$\mathbf{B} \quad r = \frac{v^2}{a}$$

F

**D** 
$$r = \frac{\sqrt{a}}{v}$$

**49.** An engraver charges a \$3 set-up fee and \$0.25 per word. Which table shows the total price pfor w words?

	W	p
13	15	\$3
	20	\$4.25
	25	\$5.50
	30	\$7.75

H	w	P
	15	\$3.75
	20	\$5
	25	\$6.25
	30	\$8.50

G	w	P
	15	\$6.75
	20	\$7
	25	\$7.25
	30	\$7.50

		1
(62)	W	p
	15	\$6.75
	20	\$8
	25	\$9.25
	30	\$10.50

**50. SHORT RESPONSE** The table shows the items in stock at the school store the first day of class. What is the probability that an item chosen at random was a notebook?

Item	Number Purchased
pencil	57
pen	38
eraser	6
folder	25
notebook	18

**51.** Solve for *n*.

$$|2n-3|=5$$

**A** 
$$\{-4, -1\}$$

**B** 
$$\{-1, 4\}$$

### **Spiral Review**

Solve each compound inequality. Then graph the solution set. (Lesson 5-4)

**52.** 
$$b + 3 < 11$$
 and  $b + 2 > -3$ 

**53.** 
$$6 \le 2t - 4 \le 8$$

**54.** 
$$2c - 3 \ge 5$$
 or  $3c + 7 \le -5$ 

- 55. FINANCIAL LITERACY In a recent year, the sum of the number of \$2 bills and \$50 bills in circulation was 1,857,573,945. The number of \$50 bills was 494,264,809 more than the number of \$2 bills. How many of each type of bill was in circulation? (Lesson 5-3)
- **56. GEOMETRY** One angle of a triangle measures 10° more than the second. The measure of the third angle is twice the sum of the measure of the first two angles. Find the measure of each angle. (Lesson 2-4)

Solve each equation. Then check your solution. (Lesson 2-2)

**57.** 
$$c - 7 = 11$$

**58.** 
$$2w = 24$$

**59.** 
$$9 + p = -11$$

**60.** 
$$\frac{t}{5} = 20$$

### **Skills Review**

Graph each equation. (Lesson 3-1)

**61.** 
$$y = 4x - 1$$

**62.** 
$$y - x = 3$$

**63.** 
$$2x - y = -4$$

**64.** 
$$3y + 2x = 6$$

**65.** 
$$4y = 4x - 16$$

**66.** 
$$2y - 2x = 8$$

**67.** 
$$-9 = -3x - y$$

**68.** 
$$-10 = 5y - 2x$$

# 5-6

### Then

You graphed linear equations. (Lesson 3-1)

#### Now

- Graph linear inequalities on the coordinate plane.
- Solve inequalities by graphing.

#### New Vocabulary

boundary half-plane closed half-plane open half-plane

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# **Graphing Inequalities** in Two Variables

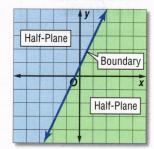
### Why?

Hannah has budgeted \$35 every three months for car maintenance. From this she must buy oil costing \$3 and filters that cost \$7 each. How much oil and how many filters can Hannah buy and stay within her budget?



**Graph Linear Inequalities** The graph of a linear inequality is the set of points that represent all of the possible solutions of that inequality. An equation defines a **boundary**, which divides the coordinate plane into two **half-planes**.

The boundary may or may not be included in the graph of an inequality. When it is included, the solution is a **closed half-plane**. When not included, the solution is an **open half-plane**.



### Key Concept

### **Graphing Linear Inequalities**

FOLDABLE

- Step 1 Graph the boundary. Use a solid line when the inequality contains  $\leq$  or  $\geq$ . Use a dashed line when the inequality contains < or >.
- Step 2 Use a test point to determine which half-plane should be shaded.
- Step 3 Shade the half-plane that contains the solution.

### EXAMPLE 1

### Graph an Inequality (< or >)

Graph 3x - y < 2.

**Step 1** First, solve for y in terms of x.

$$3x - y < 2$$

$$-y < -3x + 2$$

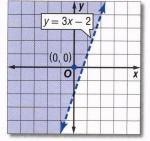
$$y > 3x - 2$$

Then, graph y = 3x - 2. Because the inequality involves >, graph the boundary with a dashed line.

**Step 2** Select a test point in either half-plane. A simple choice is (0, 0).

$$3x - y < 2$$
 Original inequality  
 $3(0) - 0 < 2$   $x = 0$  and  $y = 0$   
 $0 < 2$  true

Step 3 So, the half-plane containing the origin is the solution. Shade this half-plane.



Check Your Progress Graph each inequality.

**1A.** 
$$y > \frac{1}{2}x + 3$$

**1B.** 
$$x - 1 > y$$

### StudyTip

#### **Selecting a Test Point**

When selecting a test point, a standard choice is the origin because it offers easy calculations. However, if it lies on the border, you must choose another point that is not on the border.

#### Graph an Inequality ( $\leq$ or $\geq$ ) **EXAMPLE 2**

Graph 
$$x + 5y \le 10$$
.

**Step 1** Solve for y in terms of x.

$$x + 5y \le 10$$
 Original inequality

$$5y \le -x + 10$$
 Subtract x from each side and simplify.

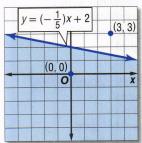
$$y \le -\frac{1}{5}x + 2$$
 Divide each side by 5.

Graph  $y = -\frac{1}{5}x + 2$ . Because the inequality symbol is  $\leq$ , graph the boundary with a solid line.

Select a test point. Let's use (3, 3). Substitute the values into the original inequality.

$$x + 5y \le 10$$
 Original inequality  
 $3 + 5(3) \le 10$   $x = 3$  and  $y = 3$   
 $18 \le 10$  Simplify.

**Step 3** Since this statement is false, shade the other half-plane.





Check Your Progress Graph each inequality.

**2A.** 
$$x - y \le 3$$

**2B.** 
$$2x + 3y \ge 18$$

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Solve Linear Inequalities We can use a coordinate plane to solve inequalities with one variable.

#### **Solve Inequalities From Graphs EXAMPLE 3**

Use a graph to solve 3x + 5 < 14.

First graph the boundary, which is the related equation. Replace the inequality sign with an equals sign, and solve for x.

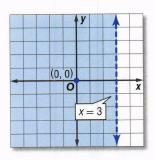
$$3x + 5 < 14$$
 Original inequality  $3x + 5 = 14$  Change  $<$  to  $=$ . Subtract 5 from each side and simplify.  $x = 3$  Divide each side by 3.

Graph x = 3 with a dashed line.

**Step 2** Choose (0, 0) as a test point. These values in the original inequality give us 5 < 14.

Since this statement is true, shade the half-plane Step 3 that contains the point (0, 0).

> Notice that the x-intercept of the graph is at 3. Since the half-plane to the left of the *x*-intercept is shaded, the solution is x < 3.





Check Your Progress Use a graph to solve each inequality.

**3A.** 
$$4x - 3 \ge 17$$

**3B.** 
$$-2x + 6 > 12$$

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### Real-World Link

As a supplement to traditional yearbooks, many schools are producing digital versions. They include features that allow you to click on a picture and see a short video clip.

Source: eSchool News

### **Problem-SolvingTip**

Use a Graph You can use a graph to visualize data, analyze trends, and make predictions.

When using inequalities to solve real-world problems, the domain and the range are often restricted to nonnegative or whole numbers.

### Real-World EXAMPLE 4 Write and Solve an Inequality

CLASS PICNIC A yearbook company promises to give the junior class a picnic if they spend at least \$28,000 on yearbooks and class rings. Each yearbook costs \$35, and each class ring costs \$140. How many yearbooks and class rings must the junior class buy to get their picnic?

**Understand** You know the cost of each item and the minimum amount the class needs to spend.

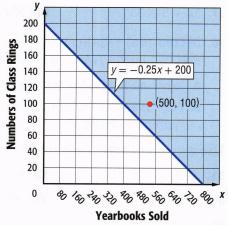
**Plan** Let x = the number of yearbooks and y = the number of class rings the class must buy. Write an inequality.

\$35		the number				the number	is at	
\$35	times	of yearbooks	plus	\$140	times	of rings	least	\$28,000.
35		X	+	140		y	<b>&gt;</b>	28,000

**Solve** Solve for y in terms of x.

$$35x + 140y - 35x \ge 28,000 - 35x$$
 Subtract 35x from each side.   
  $140y \ge -35x + 28,000$  Divide each side by 140.   
  $\frac{140y}{140} \ge \frac{-35x}{140} + \frac{28000}{140}$  Simplify.   
  $y \ge -0.25x + 200$  Simplify.

Because the yearbook company cannot sell a negative number of items, the domain and range must be nonnegative numbers. Graph the boundary with a solid line. If we test (0, 0), the result is  $0 \ge 28,000$ , which is false. Shade the closed half-plane that does not include the origin. One solution is (500, 100), or 500 yearbooks and 100 class rings.



**Check** If we test (500, 100), the result is  $100 \ge 75$ , which is true. Because the company cannot sell a fraction of an item, only points with wholenumber coordinates can be solutions.

### **Check Your Progress**

**4.** MARATHONS Neil wants to run a marathon at a pace of at least 6 miles per hour. Write and graph an inequality for the miles y he will run in x hours.

### **Check Your Understanding**

### Examples 1 and 2

Graph each inequality.

pp. 315-316

1. 
$$y > x + 3$$

**2.** 
$$y \ge -8$$

**3.** 
$$x + y > 1$$

**4.** 
$$y \le x - 6$$

**5.** 
$$y < 2x - 4$$

**6.** 
$$x - y \le 4$$

### **Example 3** p. 316

Use a graph to solve each inequality.

7. 
$$7x + 1 < 15$$

**8.** 
$$-3x - 2 \ge 11$$

**9.** 
$$3y - 5 \le 34$$

**10.** 
$$4y - 21 > 1$$

### Example 4 p. 317

11. FINANCIAL LITERACY The surf shop has a weekly overhead of \$2300.

- **a.** Write an inequality to describe this situation.
- b. How many skimboards and longboards must the shop sell each week to make a profit?



### **Practice and Problem Solving**

= Step-by-Step Solutions begin on page R12. Extra Practice begins on page 815.

### **Examples 1 and 2** pp. 315-316

Graph each inequality.

**12.** 
$$y < x - 3$$

**13.** 
$$y > x + 12$$

**14.** 
$$y \ge 3x - 1$$

**15.** 
$$y \le -4x + 12$$

**16.** 
$$6x + 3y > 12$$

17. 
$$2x + 2y < 18$$

**18.** 
$$5x + y > 10$$

**19.** 
$$2x + y < -3$$

**20.** 
$$-2x + y \ge -4$$

**21.** 
$$8x + y \le 6$$

**22.** 
$$10x + 2y \le 14$$

**23.** 
$$-24x + 8y \ge -48$$

### Example 3 p. 316

Use a graph to solve each inequality.

**24.** 
$$10x - 8 < 22$$

**25.** 
$$20x - 5 > 35$$

**26.** 
$$4y - 77 \ge 23$$

**27.** 
$$5y + 8 \le 33$$

**28.** 
$$35x + 25 < 6$$

**29.** 
$$14x - 12 > -31$$

### **Example 4**

p. 317

30. **DECORATING** Sybrina is decorating her bedroom. She has \$300 to spend on paint and bed linens. A gallon of paint costs \$14, while a set of bed linens costs \$60.

- **a.** Write an inequality for this situation.
- b. How many gallons of paint and bed linen sets can Sybrina buy and stay within her budget?

Use a graph to solve each inequality.

**31.** 
$$3x + 2 < 0$$

**32.** 
$$4x - 1 > 3$$

**33.** 
$$-6x - 8 \ge -4$$

**34.** 
$$-5x + 1 < 3$$

**35.** 
$$-7x + 13 < 10$$

**36.** 
$$-4x - 4 \le -6$$

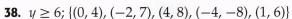


**SOCCER** The girls' soccer team wants to raise \$2000 to buy new goals. How many of each item must they sell to buy the goals?

- **a.** Write an inequality that represents this situation.
- **b.** Graph this inequality.
- **c.** Make a table of values that shows at least five possible solutions.
- **d.** Plot the solutions from part **c**.



Graph each inequality. Determine which of the ordered pairs are part of the solution set for each inequality.



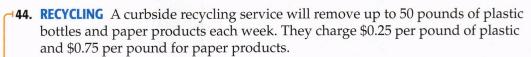
39 
$$x < -4$$
; {(2, 1), (-3, 0), (0, -3), (-5, -5), (-4, 2)}

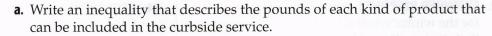
**40.** 
$$2x - 3y \le 1$$
; {(2, 3), (3, 1), (0, 0), (0, -1), (5, 3)}

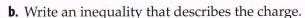
**41.** 
$$5x + 7y \ge 10$$
;  $\{(-2, -2), (1, -1), (1, 1), (2, 5), (6, 0)\}$ 

**42.** 
$$-3x + 5y < 10$$
; {(3, -1), (1, 1), (0, 8), (-2, 0), (0, 2)}

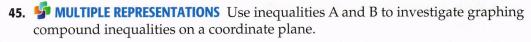
**43.** 
$$2x - 2y \ge 4$$
; {(0, 0), (0, 7), (7, 5), (5, 3), (2, -5)}







d. Compare the two graphs.



**A.** 
$$7(y+6) \le 21x + 14$$

**B.** 
$$-3y \le 3x - 12$$

- **a. NUMERICAL** Solve each inequality for *y*.
- b. GRAPHICAL Graph both inequalities on one graph. Shade the half-plane that makes A true in red. Shade the half-plane that makes B true in blue.
- c. VERBAL What does the overlapping region represent?



### Real-World Link

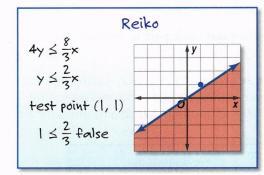
The energy saved when recycling one glass bottle is enough to light a traditional light bulb for four hours.

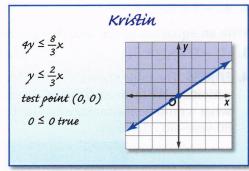
Source: PlanetPals

### H.O.T. Problems

Use Higher-Order Thinking Skills

**46. FIND THE ERROR** Reiko and Kristin are solving  $4y \le \frac{8}{3}x$  by graphing. Is either of them correct? Explain your reasoning.





- **47. CHALLENGE** Graph y > |x + 5|.
- **48. REASONING** Explain why a point on the boundary should not be used as a test point.
- **49. OPEN ENDED** Write a two-variable inequality with a restricted domain and range to represent a real-world situation. Give the domain and range, and explain why they are restricted.
- **50. WRITING IN MATH** Summarize the steps to graph an inequality in two variables.

### **Standardized Test Practice**

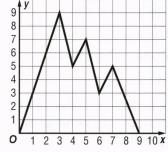
**51.** What is the domain of this function?

**A**  $\{x \mid 0 \le x \le 3\}$ 

**B**  $\{x \mid 0 \le x \le 9\}$ 

**C**  $\{y \mid 0 \le y \le 9\}$ 

**D**  $\{y \mid 0 \le y \le 3\}$ 



**52. EXTENDED RESPONSE** An arboretum will close for the winter when all of the trees have lost their leaves. The table shows the number of trees each day that still have leaves.

Day	5	10	15	20
Trees with Leaves	325	260	195	130

- **a.** Write an equation that represents the number of trees with leaves *y* after *d* days.
- **b.** Find the *y*-intercept. What does it mean in the context of this problem?
- **c.** After how many days will the arboretum close? Explain how you got your answer.

**53.** Which inequality best represents the statement below?

A jar contains 832 gumballs. Ebony's guess was within 46 pieces.

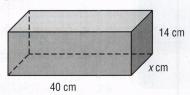
F 
$$|g - 832| \le 46$$

**G** 
$$|g + 832| \le 46$$

H 
$$|g - 832| \ge 46$$

J 
$$|g + 832| \ge 46$$

**54. GEOMETRY** If the rectangular prism has a volume of  $10,080 \text{ cm}^3$ , what is the value of x?



A 12

**B** 14

**C** 16

**D** 18

### **Spiral Review**

Solve each open sentence. (Lesson 5-5)

**55.** 
$$|y-2| > 4$$

**56.** 
$$|t-6| \le 5$$

**57.** 
$$|3+d|<-4$$

Solve each compound inequality. (Lesson 5-4)

**58.** 
$$4c - 4 < 8c - 16 < 6c - 6$$

**59.** 
$$5 < \frac{1}{2}p + 3 < 8$$

**60.** 
$$0.5n \ge -7 \text{ or } 2.5n + 2 \le 9$$

Write an equation of the line that passes through each pair of points. (Lesson 4-2)

**61.** 
$$(1, -3)$$
 and  $(2, 5)$ 

**62.** 
$$(-2, -4)$$
 and  $(-7, 3)$ 

**63.** 
$$(-6, -8)$$
 and  $(-8, -5)$ 

**64. FITNESS** The table shows the maximum heart rate to maintain during aerobic activities. Write an equation in function notation for the relation. Determine what would be the maximum heart rate to maintain in aerobic training for an 80-year-old. (Lesson 3-5)

Age (yr)	20	30	40	50	60	70
Pulse rate (beats/min)	175	166	157	148	139	130

### **Skills Review**

**65. WORK** The formula  $s = \frac{w - 10r}{m}$  is used to find keyboarding speeds. In the formula, s represents the speed in words per minute, w the number of words typed, r the number of errors, and m the number of minutes typed. Solve for r. (Lesson 2-8)

- Other Calculator Keystrokes
- Graphing Technology Personal Tutor

You can use a graphing calculator to investigate the graphs of inequalities.

**ACTIVITY 1** 

**Less Than** 

Graph  $y \leq 2x + 5$ .

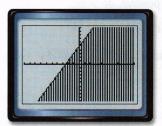
Clear all functions from the Y= list.

KEYSTROKES: Y= CLEAR

Graph  $y \le 2x + 5$  in the standard window.

KEYSTROKES: 2  $X,T,\theta,n$  + 5  $\blacktriangleleft$   $\blacktriangleleft$   $\blacktriangleleft$   $\blacktriangleleft$  ENTER ENTER ENTER Zoom 6

All ordered pairs for which y is less than or equal to 2x + 5 lie below or on the line and are solutions.



[-10, 10] scl: 1 by [-10, 10] scl: 1

### **ACTIVITY 2**

**Greater Than** 

Graph  $y - 2x \ge 5$ .

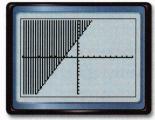
Clear the graph that is currently displayed.

KEYSTROKES: Y= CLEAR

Rewrite  $y - 2x \ge 5$  as  $y \ge 2x + 5$  and graph it.

KEYSTROKES: 2  $X,T,\theta,n$  + 5  $\blacktriangleleft$   $\blacktriangleleft$   $\blacktriangleleft$   $\blacktriangleleft$  ENTER ENTER Zoom 6

All ordered pairs for which *y* is *greater than or equal to* 2x + 5 lie above or on the line and are solutions.



[-10, 10] scl: 1 by [-10, 10] scl: 1

### **Exercises**

- 1. Compare and contrast the two graphs shown above.
- **2.** Graph  $y \ge -3x + 1$  in the standard viewing window. Using your graph, name four solutions of the inequality.
- **3.** Suppose student water park tickets cost \$16, and adult water park tickets cost \$20. You would like to buy at least 10 tickets but spend no more than \$200.
  - **a.** Let x = number of student tickets and y = number of adult tickets. Write two inequalities, one representing the total number of tickets and the other representing the total cost of the tickets.
  - **b.** Graph the inequalities. Use the viewing window [0, 20] scl: 1 by [0, 20] scl: 1.
  - **c.** Name four possible combinations of student and adult tickets.

# **Study Guide and Review**

### **Chapter Summary**

### **Key Concepts**

**Solving One-Step Inequalities** (Lessons 5-1 and 5-2)

For all numbers a, b, and c, the following are true.

- If a > b and c is positive, ac > bc.
- If a > b and c is negative, ac < bc.

Multi-Step and Compound Inequalities (Lessons 5-3 and 5-4)

- Multi-step inequalities can be solved by undoing the operations in the same way you would solve a multistep equation.
- A compound inequality containing and is only true if both inequalities are true.
- A compound inequality containing or is true if at least one of the inequalities is true.

**Absolute Value Inequalities** (Lesson 5-5)

- The absolute value of any number x is its distance from zero on a number line and is written as |x|. If  $x \ge 0$ , then |x| = x. If x < 0, then |x| = -x.
- If |x| < n and n > 0, then -n < x < n.
- If |x| > n and n > 0, then x > n or x < -n.

**Inequalities in Two Variables** (Lesson 5-6)

To graph an inequality:

- **Step 1** Graph the boundary. Use a solid line when the inequality contains  $\leq$  or  $\geq$ . Use a dashed line when the inequality contains < or >.
- **Step 2** Use a test point to determine which half-plane should be shaded.
- **Step 3** Shade the half-plane.

## FOLDABLES Study Organizer

Be sure the Key Concepts are noted in your Foldable.



### **Key Vocabulary**

**boundary** (p. 315)

closed half-plane (p. 315)

compound inequality (p. 304)

half plane (p. 315)

intersection (p. 304)

open half-plane (p. 315)

set-builder notation (p. 284)

**union** (p. 305)

### **Vocabulary Check**

State whether each sentence is true or false. If false, replace the underlined term to make a true sentence.

- 1. Set-builder notation is a less concise way of writing a solution set.
- **2.** There are two types of compound inequalities.
- 3. The graph of a compound inequality containing and shows the <u>union</u> of the individual graphs.
- **4.** A compound inequality containing *or* is true if one or both of the inequalities is true. Its graph is the union of the graphs of the two inequalities.
- **5.** The graph of an inequality of the form y < ax + bis a region on the coordinate plane called a half-
- 6. A point defines the boundary of an open halfplane.
- 7. The boundary is the graph of the equation of the line that defines the edge of each half-plane.
- **8.** The solution set to the inequality  $y \ge x$  includes the boundary.
- 9. When solving an inequality, multiplying each side by a negative number reverses the inequality symbol.
- 10. The graph of a compound inequality that contains and is the intersection of the graphs of the two inequalities.

### **Lesson-by-Lesson Review**

### Solving Inequalities by Addition and Subtraction (pp. 283–288)

Solve each inequality. Then graph it on a number line.

11. 
$$w - 4 > 9$$

**12.** 
$$x + 8 \le 3$$

**13.** 
$$6 + h < 1$$

**14.** 
$$-5 < a + 2$$

**15.** 
$$13 - p \ge 15$$

**16.** 
$$y + 1 \le 8$$

### **EXAMPLE 1**

Solve x - 9 < -4. Then graph it on a number

$$x - 9 < -4$$

**Original inequality** 

$$x - 9 + 9 < -4 + 9$$

Add 9 to each side.

Simplify.

The solution set is 
$$\{x \mid x < 5\}$$
.



### Solving Inequalities by Multiplication and Division (pp. 290–295)

Solve each inequality. Check your solution.

**18.** 
$$\frac{1}{3}x > 6$$

19. 
$$\frac{1}{5}g \ge -4$$

**20.** 
$$4p < 32$$

**21.** 
$$-55 \le -5w$$

**22.** 
$$-2m > 100$$

**23.** 
$$\frac{2}{3}t < -48$$

24. MOVIE RENTAL Jack has no more than \$24 to spend on DVDs for a party. Each DVD rents for \$4. Find the maximum number of DVDs Tack can rent for his party.

### **EXAMPLE 2**

Solve -14h < 56. Check your solution.

$$-14h < 56$$

**Original inequality** 

$$\frac{-14h}{-14} > \frac{56}{-14}$$

Divide each side by -14.

$$\{h \, | \, h > -4 \}$$

Simplify.

**CHECK** To check, substitute three different values into the original inequality: -4, a number less than -4, and a number greater than -4.

#### 5-3 **Solving Multi-Step Inequalities** (pp. 296–301)

Solve each inequality. Check your solution.

**25.** 
$$3h - 7 < 14$$

**26.** 
$$4 + 5b > 34$$

**27.** 
$$18 \le -2x + 8$$

**28.** 
$$\frac{t}{3} - 6 > -4$$

- 29. Four times a number decreased by 6 is less than -2. Define a variable, write an inequality, and solve for the number.
- **30. TICKET SALES** The drama club collected \$160 from ticket sales for the spring play. They need to collect at least \$400 to pay for new lighting for the stage. If tickets sell for \$3 each, how many more tickets need to be sold?

### **EXAMPLE 3**

Solve -6y - 13 > 29. Check your solution.

$$-6y - 13 > 29$$

**Original inequality** 

$$-6y - 13 + 13 > 29 + 13$$

Add 13 to each side.

$$-6y > 42$$

Simplify.

$$\frac{-6y}{-6} < \frac{42}{-6}$$

Divide each side by -6 and change > to <.

$$y < -7$$

Simplify.

The solution set is  $\{y \mid y < -7\}$ .

**CHECK** 
$$-6y - 13 > 29$$

**Original inequality** 

$$-6(-10) - 13 \stackrel{?}{>} 29$$

$$6(-10) - 13 \stackrel{?}{>} 29$$

Substitute -10 for y.

Simplify.

# **Study Guide and Review**

#### 5-4 **Solving Compound Inequalities** (pp. 304–309)

Solve each compound inequality. Then graph the solution set.

**31.** 
$$m - 3 < 6$$
 and  $m + 2 > 4$ 

**32.** 
$$-4 < 2t - 6 < 8$$

**33.** 
$$3x + 2 \le 11$$
 or  $5x - 8 > 22$ 

**34. KITES** A kite can be flown in wind speeds no less than 7 miles per hour and no more than 16 miles per hour. Write an inequality for the wind speeds at which the kite can fly.

### **EXAMPLE 4**

Solve -3w + 4 > -8 and 2w - 11 > -19. Then graph the solution set.

$$-3w + 4 > -8$$

$$2w - 11 > -19$$

$$w > -4$$

To graph the solution set, graph w < 4 and graph w > -4. Then find the intersection.

#### 5-5 Inequalities Involving Absolute Value (pp. 310-314)

Solve each inequality. Then graph the solution set.

**35.** 
$$|x-4| < 9$$

**36.** 
$$|p+2| > 7$$

**37.** 
$$|2c + 3| \le 11$$

**38.** 
$$|f-9| \ge 2$$

**39.** 
$$|3d-1| \le 8$$

**40.** 
$$\left| \frac{4b-2}{3} \right| < 12$$

**41.** 
$$\left| \frac{2t+6}{2} \right| > 10$$
 **42.**  $\left| -4y-3 \right| < 13$ 

**42.** 
$$|-4y-3| < 13$$

**43.** 
$$|m+19| \le 1$$

**44.** 
$$|-k-7| \ge 4$$

### **EXAMPLE 5**

Solve |x - 6| < 9. Then graph the solution set.

Case 1 
$$x - 6$$
 is

Case 2 
$$x - 6$$
 is negative.

nonnegative. 
$$x - 6 < 9$$

$$-(x-6) < 9$$
$$x > -3$$

$$x < 15$$
  
The solution set is  $\{x \mid -3 < x < 15\}$ .



#### 5-6 **Graphing Inequalities in Two Variables** (pp. 315-320)

Graph each inequality.

**45.** 
$$y > x - 3$$

**46.** 
$$y < 2x + 1$$

**47.** 
$$3x - y \le 4$$

**48.** 
$$y \ge -2x + 6$$

**49.** 
$$5x - 2y < 10$$

**50.** 
$$3x + 4y > 12$$

Graph each inequality. Determine which of the ordered pairs are part of the solution set for each inequality.

**51.** 
$$y \le 4$$
; {(3, 6), (1, 2), (-4, 8), (3, -2), (1, 7)}

**52.** 
$$-2x + 3y \ge 12$$
; {(-2, 2), (-1, 1), (0, 4), (2, 2)}





### **EXAMPLE 6**

Graph 
$$2x - y > 3$$
.

Solve for *y* in terms of *x*.

$$2x - y > 3$$

$$-1/2 > -2x + 3$$

$$-y > -2x + 3$$

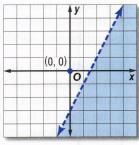
$$y < 2x - 3$$

Multiply each side by 
$$-1$$
.

Graph the boundary using a dashed line. Choose (0, 0) as a test point.

$$2(0) - 0 \stackrel{?}{>} 3$$

Since 0 is not greater than 3, shade the plane that does not contain (0, 0).



Solve each inequality. Then graph it on a number line.

1. 
$$x - 9 < -4$$

**2.** 
$$6p \ge 5p - 3$$

**3. MULTIPLE CHOICE** Drew currently has 31 comic books in his collection. His friend Connor has 58 comic books. How many more comic books does Drew need to add to his collection in order to have a larger collection than Connor?

A no more than 21

**B** 27

C at least 28

D more than 30

Solve each inequality. Check your solution.

**4.** 
$$\frac{1}{5}h > 3$$

5. 
$$7w \le -42$$

**6.** 
$$-\frac{2}{3}t \ge 24$$

7. 
$$-9m < -36$$

**8.** 
$$3c - 7 < 11$$

**9.** 
$$\frac{g}{4} + 3 \le -9$$

**10.** 
$$-2(x-4) > 5x - 13$$

11. **Z00** The 8th grade science class is going to the zoo. The class can spend up to \$300 on admission.

Zoo Admission								
Visitor	Cost							
Student	\$8							
Adult	\$10							

- **a.** Write an inequality for this situation.
- **b.** If there are 32 students in the class and 1 adult will attend for every 8 students, how much will admission be?

Solve each compound inequality. Then graph the solution set.

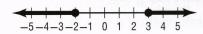
**12.** 
$$y - 8 < -3$$
 or  $y + 5 > 19$ 

**13.** 
$$-11 \le 2h - 5 \le 13$$

**14.** 
$$3z - 2 > -5$$
 and  $7z + 4 < -17$ 

Define a variable, write an inequality, and solve the problem. Check your solution.

- 15. The difference of a number and 4 is no more than 8.
- **16.** Nine times a number decreased by four is at least twenty-three.
- 17. MULTIPLE CHOICE Write a compound inequality for the graph shown below.



**F** 
$$-2 \le x < 3$$

H 
$$x < -2$$
 or  $x \ge 3$ 

**G** 
$$x \le -2$$
 or  $x \ge 3$ 

$$J -2 < x \le 3$$

Solve each inequality. Then graph the solution set.

**18.** 
$$|p-5| < 3$$

**19.** 
$$|2f + 7| \ge 21$$

**20.** 
$$|-4m+3| \le 15$$

**20.** 
$$|-4m+3| \le 15$$
 **21.**  $\left|\frac{x-3}{4}\right| > 5$ 

- **22. RETAIL** A sporting goods store is offering a \$15 coupon on any pair of shoes.
  - **a.** The most and least expensive pairs of shoes are \$149.95 and \$24.95. What is the range of costs for customers with coupons?
  - **b.** When buying a pair of \$109.95 shoes, you can use a coupon or a 15% discount. Which option is best?

Graph each inequality.

**23.** 
$$y < 4x - 1$$

**24.** 
$$2x + 3y \ge 12$$

- **25.** Graph y > -2x + 5. Then determine which of the ordered pairs in  $\{(-2, 0), (-1, 5), (2, 3), (7, 3)\}$  are in the solution set.
- **26. PRESCHOOL** Mrs. Jones is buying new books and puzzles for her preschool classroom. Each book costs \$6, and each puzzle costs \$4. Write and graph an inequality to determine how many books and puzzles she can buy for \$96.

# **Preparing for Standardized Tests**

# Write and Solve an Inequality

Many multiple-choice items will require writing and solving inequalities. Follow the steps below to help you successfully solve these types of problems.

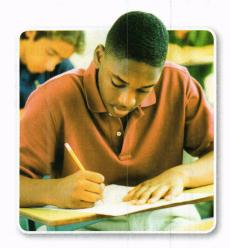
### Strategies for Writing and Solving Inequalities

### Step 1

Read the problem statement carefully.

### Ask yourself:

- What am I being asked to solve?
- What information is given in the problem?
- What are the unknowns for which I need to solve?



### Step 2

Translate the problem statement into an inequality.

- Assign variables to the unknown(s).
- Write the word sentence as a mathematical number sentence looking for words such as greater than, less than, no more than, up to, or at least to indicate the type of inequality as well as where to place the inequality sign.

### Step 3

Solve the inequality.

- Solve for the unknowns in the inequality.
- Remember that multiplying or dividing each side by a negative number reverses the direction of the inequality.
- Check your answer to make sure it makes sense.

### **EXAMPLE**

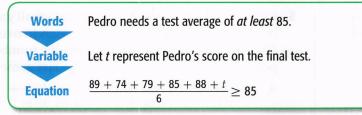
Read the problem. Identify what you need to know. Then use the information in the problem to solve. Show your work.

Pedro has earned scores of 89, 74, 79, 85, and 88 on his tests this semester. He needs a test average of at least 85 in order to earn an A for the semester. There will be one more test given this semester.

- A Write an inequality to model the situation.
- **B** What score must he have on his final test to earn an A for the semester?

Read the problem carefully. You are given Pedro's first 5 test scores and told that he needs an average of at least 85 after his next test to earn an A for the semester.

### **a.** Write the inequality.



### **b.** Solve the inequality for t.

$$\frac{89 + 74 + 79 + 85 + 88 + t}{6} \ge 85$$

$$89 + 74 + 79 + 85 + 88 + t \ge 85(6)$$

$$415 + t \ge 510$$

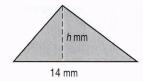
$$t \ge 95$$

So, Pedro's final test score must be greater than or equal to 95 in order for him to earn an A for the semester.

### **Exercises**

Read each problem. Identify what you need to know. Then use the information in the problem to solve.

- 1. Craig has \$20 to order a pizza. The pizza costs \$12.50 plus \$0.95 per topping. If there is also a \$3 deliver fee, how many toppings can Craig order?
- **2.** To join an archery club, Nina had to pay an initiation fee of \$75, plus \$40 per year in membership dues.
  - **a.** Write an equation to model the total cost, *y*, of belonging to the club for *x* years.
  - **b.** How many years will it take her to spend more than \$400 to belong to the club?
- **3.** The area of the triangle below is no more than 84 square millimeters. What is the height of the triangle?



- **4.** Rosa earns \$200 a month delivering newspapers, plus an average of \$11 per hour babysitting. If her goal is to earn at least \$295 this month, how many hours will she have to babysit?
- **5.** To earn money for a new bike, Ethan is selling some of his baseball cards. He has saved \$245. If the bike costs \$1400, and he can sell 154 cards, for how much money will he need to sell each card to reach his goal?
- **6.** In a certain lacrosse league, there can be no more than 22 players on each team, and no more than 10 teams per age group. There are 6 age groups.
  - **a.** Write an inequality to represent this situation.
  - **b.** What is the greatest number of players that can play lacrosse in this league?
- **7.** Sarah has \$120 to shop for herself and to buy some gifts for 6 of her friends. She has purchased a shirt for herself for \$32. What is the maximum that she can spend on each friend?

### **Multiple Choice**

Read each question. Then fill in the correct answer on the answer document provided by your teacher or on a sheet of paper.

1. Miguel received a \$100 gift certificate for a graduation gift. He wants to buy a CD player that costs \$38 and CDs that cost \$12 each. Which of the following inequalities represents how many CDs Miguel can buy?

A  $n \leq 6$ 

**B**  $n \ge 5$ 

C n < 5

**D**  $n \leq 5$ 

2. Craig is paid time-and-a-half for any additional hours over 40 that he works.

Time	Pay Rate
Up to 40 hours	\$12.80/hr
Additional hours worked over 40	\$19.20/hr

If Craig's goal is to earn at least \$600 next week, what is the minimum number of hours he needs to work?

F 43 hours

H 45 hours

G 44 hours

J 46 hours

**3.** Which equation has a slope of  $-\frac{2}{3}$  and a y-intercept of 6?

**4.** The highest score that is on record on a video game is 10,219 points. The lowest score on record is 257 points. Which of the following inequalities best shows the range of scores recorded on the game?

**F**  $x \le 10,219$ 

**G**  $x \ge 257$ 

**H** 257 < x < 10,219

J  $257 \le x \le 10,219$ 

**5.** Kyle scored 14 points in his last basketball game, bringing his total points for the season to over 100. Which number line represents the number of points Kyle had scored prior to the last game?

++++ 79 80 81 82 83 84 85 86 87 88 89 90 91

79 80 81 82 83 84 85 86 87 88 89 90 91

79 80 81 82 83 84 85 86 87 88 89 90 91

79 80 81 82 83 84 85 86 87 88 89 90 91

6. The girls' volleyball team is selling T-shirts and pennants to raise money for new uniforms. The team hopes to raise more than \$250.

Item	Price .
T-shirt	\$10
Pennant	\$4

Which of the following combinations of items sold would meet this goal?

F 16 T-shirts and 20 pennants

**G** 20 T-shirts and 12 pennants

H 18 T-shirts and 18 pennants

J 15 T-shirts and 25 pennants

7. What type of line does not have a defined slope?

A horizontal

C perpendicular

**B** parallel

**D** vertical

**8.** Which expression below illustrates the Associative Property?

 $\mathbf{F}$  abc = bac

**G** 2(x-3) = 2x-6

**H** (p+3) - t = p + (3-t)

 $\mathbf{J} \quad 5 + (-5) = 0$ 

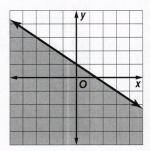
### Test-TakingTip

Question 2 You can check your answer by finding Craig's earnings for the hours worked.

### Short Response/Gridded Response

Record your answers on the answer sheet provided by your teacher or on a sheet of paper.

- **9.** Solve  $-4 < 3x + 8 \le 23$ .
- **10. GRIDDED RESPONSE** Tien is saving money for a new television. She needs to save at least \$720 to pay for her expenses. Each week Tien saves \$50 toward her new television. How many weeks will it take so she can pay for the television?
- 11. Write an inequality that best represents the graph.



- **12.** Solve |x-4| < 2.
- **13. GRIDDED RESPONSE** Daniel wants to ship a set of golf clubs and several boxes of golf balls in a box that can hold up to 20 pounds. If the set of clubs weighs 9 pounds and each box of golf balls weighs 12 ounces, how many boxes of golf balls can Daniel ship?
- **14.** Graph the solution set for the inequality  $3x - 6 \le 4x - 4 \le 3x + 1.$

15. Write an equation that represents the data in the table.

X	у
3	12.5
4	16
5	19.5
6	23
7	26.5

**16.** A sporting goods company near the beach rents bicycles for \$10 plus \$5 per hour. Write an equation in slope-intercept form that shows the total cost, y, of renting a bicycle for x hours. How much would it cost Emily to rent a bicycle for 6 hours?

### **Extended Response**

Record your answers on a sheet of paper. Show your work.

- **17.** Theresa is saving money for a vacation. She needs to save at least \$640 to pay for her expenses. Each week, she puts \$35 towards her vacation savings.
  - **a.** Let *w* represent the number of weeks Theresa saves money. Write an inequality to model the situation.
  - **b.** Solve the inequality from part a. What is the minimum number of weeks Theresa must save money in order to reach her goal?
  - **c.** If Theresa were to save \$45 each week instead, by how many weeks would the minimum savings time be decreased?

Need Extra Help?																	
If you missed Question	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
Go to Lesson or Page	5-3	5-2	4-1	5-4	5-1	5-6	3-3	1-3	5-4	5-2	5-6	5-5	5-3	5-4	2-1	4-2	5-2

# CHAPTER

# **Systems of Linear Equations** and Inequalities

### Then

In Chapter 2, you solved linear equations in one variable.

### Now

In Chapter 6, you will:

- Solve systems of linear equations by graphing, substitution, and elimination.
- Solve systems of linear inequalities by graphing.

### Why?

MUSIC \$1500 worth of tickets were sold for a marching band competition. Adult tickets were \$12 each, and student tickets were \$8 each. If you knew how many total tickets were sold, you could use a system of equations to determine how many adult tickets and how many student tickets were sold.

of Linear Equations and Inequalities

